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Pyramidal Neurons Switch From Integrators In Vitro to Resonators Under In Vivo-Like Conditions

Steven A. Prescott,¹ Stéphanie Ratté,² Yves De Koninck,³ and Terrence J. Sejnowski^{1,4}

¹Howard Hughes Medical Institute, Computational Neurobiology Laboratory, Salk Institute, La Jolla, California; ²Département de Physiologie, Université de Montréal, Montreal, Quebec, Canada; ³Division de Neurobiologie Cellulaire, Centre de Recherche Université Laval Robert-Giffard, Quebec, Quebec, Canada; and ⁴Division of Biological Sciences, University of California, San Diego, La Jolla, California

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Prescott SA, Ratté S, De Koninck Y, Sejnowski TJ. Pyramidal neurons switch from integrators in vitro to resonators under in vivolike conditions. J Neurophysiol 100: 3030-3042, 2008. First published October 1, 2008; doi:10.1152/jn.90634.2008. During wakefulness, pyramidal neurons in the intact brain are bombarded by synaptic input that causes tonic depolarization, increased membrane conductance (i.e., shunting), and noisy fluctuations in membrane potential; by comparison, pyramidal neurons in acute slices typically experience little background input. Such differences in operating conditions can compromise extrapolation of in vitro data to explain neuronal operation in vivo. For instance, pyramidal neurons have been identified as integrators (i.e., class 1 neurons according to Hodgkin's classification of intrinsic excitability) based on in vitro experiments but that classification is inconsistent with the ability of hippocampal pyramidal neurons to oscillate/resonate at theta frequency since intrinsic oscillatory behavior is limited to class 2 neurons. Using long depolarizing stimuli and dynamic clamp to reproduce in vivo-like conditions in slice experiments, we show that CA1 hippocampal pyramidal cells switch from integrators to resonators, i.e., from class 1 to class 2 excitability. The switch is explained by increased outward current contributed by the M-type potassium current $I_{\rm M}$, which shifts the balance of inward and outward currents active at perithreshold potentials and thereby converts the spike-initiating mechanism as predicted by dynamical analysis of our computational model. Perithreshold activation of $I_{\rm M}$ is enhanced by the depolarizing shift in spike threshold caused by shunting and/or sodium channel inactivation secondary to tonic depolarization. Our conclusions were validated by multiple comparisons between simulation and experimental data. Thus even so-called "intrinsic" properties may differ qualitatively between in vitro and in vivo conditions.

INTRODUCTION

The high level of background synaptic input received by pyramidal neurons in the intact, awake brain can significantly alter the integrative properties of those neurons (Bernander et al. 1991; Destexhe and Paré 1999; Paré et al. 1998). Destexhe and Paré (1999) reported that, on average, background synaptic input to neocortical pyramidal neurons reduced input resistance by 80% while causing a 20 mV depolarizing shift in membrane potential and a tenfold increase in the SD of voltage noise (for review, see Destexhe et al. 2003). Reducing input resistance (i.e., shunting) causes predictable shortening of both the membrane time and length constants; this in turn causes the cell to behave more like a coincidence detector and less like an integrator insofar as the neuron responds more selectively to synchronized inputs (Bernander et al. 1991; Rudolph and Destexhe 2003). Thus passive membrane properties differ between in vitro and in vivo conditions with important consequences for how neurons process information. Noise caused by synaptic input has equally unintuitive implications, for instance, on firing rate modulation by shunting inhibition (Chance et al. 2002; Prescott and De Koninck 2003) and on contrast invariance of orientation tuning in visual cortex (Anderson et al. 2000). Wolfart et al. (2005) showed in thalamic neurons that conductance noise blurs the single-spike and burst firing modes (which are classically associated with depolarized and hyperpolarized membrane potentials, respectively) and interacts with intrinsic currents to determine the neuron's transfer function. Steriade (2001) described several examples in which noise influences "intrinsic" spiking patterns. Still other discrepancies are likely to exist between in vitro and in vivo conditions.

Here we address whether CA1 pyramidal neurons exhibit class 1 or class 2 excitability according to Hodgkin's classification scheme (Hodgkin 1948): class 1 neurons can maintain arbitrarily slow firing and therefore have a continuous frequencycurrent (f-I) curve, whereas class 2 neurons cannot maintain firing below some critical rate and therefore have a discontinuous *f-I* curve. Subsequent work has shown that this phenomenological difference derives from the different dynamical mechanisms responsible for spike initiation in each cell class (Izhikevich 2007; Prescott et al. 2008; Rinzel and Ermentrout 1998). The spike-initiating mechanism, in turn, has several important implications. For instance, the phase response curve (PRC) differs between class 1 and 2 neurons (Rinzel and Ermentrout 1998): a perturbation can only advance the next spike in class 1 neurons (i.e., monophasic PRC), whereas it can advance or delay the next spike in class 2 neurons depending on when the perturbation occurs (i.e., biphasic PRC). This property affects the synchronization of neurons within a network: class 1 neurons will not synchronize in a purely excitatory network, whereas class 2 neurons will (Ermentrout 1996; Hansel et al. 1995), although class 1 neurons can be synchronized by inhibitory input (e.g., Wang and Buzsáki 1996). Moreover, because of their spike-initiating mechanism, class 1 neurons summate inputs across a broad range of frequencies, whereas class 2 neurons have a preferred input frequency to which they

Present address and address for reprint requests and other correspondence: S. A. Prescott, Dept. of Neurobiology, University of Pittsburgh, Biomedical Science Tower, W1455, 200 Lothrop St., Pittsburgh, PA 15213 (E-mail: prescott@neurobio.pitt.edu).

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resonate. Class 1 and 2 neurons have therefore been labeled integrators and resonators, respectively (Izhikevich 2007).

It seems to be commonly believed that pyramidal cells are class 1, or at least that is how they have been modeled (e.g., Wilson 1999) and the assumption is implicit in the widespread use of leaky integrate-and-fire models. But there is an unrecognized discrepancy: hippocampal CA1 pyramidal neurons do indeed have continuous f-I curves according to in vitro experiments (e.g., Gustafsson and Wigstrom 1981), consistent with class 1 excitability, but they can (under slightly different conditions) also exhibit subthreshold oscillations and resonance at 3–10 Hz or θ frequency (Hu et al. 2002; Leung and Yu 1998; Leung and Yim 1991; Pike et al. 2000), consistent with class 2 excitability. Needless to say, network oscillations are important for brain function (Buzsáki 2006) and although intrinsic resonance is not required for entrainment of pyramidal cell activity, it influences responsiveness to oscillatory input and is likely to affect θ -related phase precession (Harris et al. 2002). It is therefore critical that we understand and resolve this discrepancy so that neurons are modeled with the appropriate spike-initiating mechanism.

We reasoned that synaptic bombardment experienced in vivo causes a relative increase in outward current via shunting and activation or inactivation of currents secondary to tonic depolarization. Based on our recent work on spiking initiating dynamics (Prescott et al. 2008), a relative increase in outward current could theoretically convert neuronal excitability from class 1 to class 2. In other words, CA1 pyramidal cells that behave as integrators under in vitro conditions may behave as resonators under in vivo conditions. To investigate this, we first tested the effects of shunting and adaptation in a computational model amenable to dynamical analysis. Then, directed by specific predictions derived from modeling, we tested CA1 pyramidal neurons under different in vivo-like conditions. As we predicted, results demonstrate that "intrinsic" spike-initiating dynamics do indeed differ between in vitro and in vivo conditions because of the relative increase in outward current in vivo.

METHODS

Slicing and electrophysiology

All experiments were done in accordance with regulations of the Canadian Council on Animal Care and have been described by us previously (Prescott et al. 2006). Adult male Sprague Dawley rats were anesthetized with intraperitoneal injection of sodium pentobarbital (30 mg/kg) and perfused intracardially with ice-cold oxygenated (95% O_2 -5% CO_2) sucrose-substituted artificial cerebrospinal fluid (ACSF) containing (in mM) 252 sucrose, 2.5 KCl, 2 CaCl₂, 2 MgCl₂, 10 glucose, 26 NaHCO₃, 1.25 NaH₂PO₄, and 5 kynurenic acid. The brain was rapidly removed and sectioned coronally to give 400- μ m-thick slices, which were kept in normal oxygenated ACSF (126 mM NaCl instead of sucrose and without kynurenic acid) at room temperature until recording.

Slices were transferred to a recording chamber constantly perfused with oxygenated (95% O₂-5% CO₂) ACSF heated to 30–31°C. Pyramidal neurons in the CA1 region of hippocampus were recorded in the whole cell configuration with >80% series resistance compensation using an Axopatch 200B amplifier (Molecular Devices; Palo Alto, CA). Only data from regular spiking pyramidal cells judged healthy on the basis of three criteria (resting membrane potential less than -50 mV, spikes overshooting 0 mV, and input resistance >100 $M\Omega$) were included in analysis presented here. Average resting V was -73 ± 1 (SE) mV, and average input resistance was 159 ± 9 MΩ. Variations in resting V were eliminated by adjusting V to -70 mV through tonic current injection. Reported values of V were corrected for liquid junction potential calculated (see Barry and Lynch 1991) to be 9 mV based on the intracellular recording solution, which contained (in mM) 135 KMeSO₄, 5 KCl, 10 HEPES, and 2 MgCl₂, 4 ATP (Sigma), 0.4 GTP (Sigma) as well as 0.1% Lucifer yellow; pH was adjusted to 7.2 with KOH. Pyramidal morphology was confirmed with epifluorescence after recording. All experiments were performed in 10 μ M bicuculline methiodide (Research Biochemicals, Natick, MA), 10 μ M 6-cyano-7-nitroquinoxaline-2,3-dione (CNQX), and 40 μ M D-2-amino-5-phosphonovaleric acid (D-AP-5, Tocris Cookson, Bristol, UK) to block residual background synaptic activity.

To recreate tonic depolarization, long depolarizing current steps were injected into the cell via the recording pipette; current magnitude is reported as I_{stim} . To recreate increased membrane conductance (i.e., shunting), an artificial conductance was applied via dynamic clamp implemented with a Digidata 1200A ADC/DAC board (Molecular Devices) and DYNCLAMP2 software (Pinto et al. 2001) running on a dedicated processor; update rate was 10 kHz. For this study, we only report the effects of a single conductance level that was constant at 10 nS and was associated with a reversal potential of -70 mV; this conductance caused an average 56% reduction in input resistance. To recreate the voltage noise caused by synaptic input, noisy current (see following text) was injected into the cell, but the effects of noise were not analyzed in this study except for one experiment identified in RESULTS. Recreating the effects of background synaptic activity using dynamic clamp has been previously validated and discussed in detail elsewhere (Chance et al. 2002; Destexhe et al. 2001; Prescott et al. 2006; for review, see Prescott and De Koninck 2008).

Traces were low-passed filtered at 4 kHz and stored on videotape using a digital data recorder (VR-10B, Instrutech; Port Washington, NY). Off-line, recordings were sampled at 10 kHz on a computer using Strathclyde Electrophysiology software (J. Dempster, Department of Physiology and Pharmacology, University of Strathclyde, Glasgow, UK) and analyzed using locally designed software (De Koninck).

Simulations

Simulations were based on a modified Morris-Lecar model (Morris and Lecar 1981; Rinzel and Ermentrout 1998) that we have analyzed in detail (Prescott et al. 2008). The model is described by the following equations

$$C dV/dt = I_{stim} + I_{noise} - \bar{g}_{Na} m_{\infty}(V)(V - E_{Na}) - \bar{g}_{K,dr} w(V - E_{K})$$
$$- g_{shunt}(V - E_{shunt}) - \bar{g}_{adapt} z(V - E_{K}) \quad (I)$$
$$w(V) = w$$

$$dw/dt = \phi_w \frac{w_{\infty}(V) - w}{\tau_w(V)}$$
(2)

$$dz/dt = \left[\frac{1}{1 + e^{(\beta_z - V)/\gamma_z}} - z\right]/\tau_z$$
(3)

$$n_{\infty}(V) = 0.5 \left[1 + \tanh\left(\frac{V - \beta_m}{\gamma_m}\right) \right]$$
(4)

$$v_{\infty}(V) = 0.5 \left[1 + \tanh\left(\frac{V - \beta_w}{\gamma_w}\right) \right]$$
 (5)

$$\tau_{w}(V) = 1/\cosh\left(\frac{V-\beta_{w}}{2\cdot\gamma_{w}}\right)$$
(6)

This minimal model was used instead of more complex, higher dimensional models (e.g., Hodgkin-Huxley) because it is amenable to dynamical analysis that can be used to explain key features of the model's behavior (see following text). For example, the Morris-Lecar model neglects sodium channel inactivation since it operates on the same time scale as delayed rectifier channel activation (e.g., Kepler et al. 1992). Our model is modified from the original Morris-Lecar model primarily by the addition of adaptation. All parameters were set according past modeling studies (Prescott et al. 2006, 2008) rather than being quantitatively fit to experimental data, notwithstanding the final set of simulations presented in Figs. 8 and 9.

Unless otherwise stated, $E_{\rm Na} = 50 \text{ mV}$, $E_{\rm K} = -100 \text{ mV}$, $E_{\rm shunt} = -70 \text{ mV}$, $\bar{g}_{\rm Na} = 20 \text{ mS/cm}^2$, $\bar{g}_{\rm K,dr} = 20 \text{ mS/cm}^2$, $\phi_{\rm w} = 0.25$, $C = 2 \mu$ F/cm², $\beta_{\rm m} = -1.2 \text{ mV}$, $\gamma_{\rm m} = 18 \text{ mV}$, $\beta_{\rm w} = -9 \text{ mV}$, and $\gamma_{\rm w} = 10 \text{ mV}$. Low- and high-conductance states were simulated by changing $g_{\rm shunt}$ from 2 to 4 mS/cm². In additional simulations not reported here, the 2 mS/cm² increase in $g_{\rm shunt}$ was associated with a reversal potential of -57 mV, which more accurately reflects the net reversal potential for background synaptic activity (see following text); results were qualitatively unchanged from simulations in which the reversal potential was -70 mV. Adaptation comprised two separate currents: M-type K⁺ current with $\bar{g}_{\rm M} = 2 \text{ mS/cm}^2$, $\tau_z = 200 \text{ ms}$, $\beta_z = -30 \text{ mV}$, and $\gamma_z = 5 \text{ mV}$ and calcium-activated K⁺ current with $\bar{g}_{\rm AHP} = 1 \text{ mS/cm}^2$, $\tau_z = 200 \text{ ms}$, $\beta_z = 0 \text{ mV}$, and $\gamma_z = 5 \text{ mV}$. Activation of $I_{\rm M}$ and $I_{\rm AHP}$ were controlled separately by $z_{\rm M}$ and $z_{\rm AHP}$.

Weak noise was included in all simulations investigating membrane potential oscillations (MPOs) to replicate noise that is still present in real neurons after blockade of fast synaptic input. This noise prevents the model from being unphysiologically stable by perturbing the system from its fixed point; MPOs are generated as the system returns toward its fixed point, meaning at least some noise is necessary for the generation of irregular MPOs like those observed experimentally (Dorval and White 2005; Erchova et al. 2004; Hutcheon and Yarom 2000). Noisy current was modeled as an Ornstein-Uhlenbeck process $dI_{noise}/dt = -I_{noise}/\tau_{noise} + \sigma_{noise} N(0,1)$ where N is a random number with 0 mean and unit variance, and $\sigma_{noise} = 0.1$ or $0.01 \ \mu A/cm^2$ when $\tau_{noise} = 5$ or 500 ms, respectively, to give equivalent variance in I_{noise} which equals $\sigma^2 \tau/2$ (see Gillespie 1996). These values of σ_{noise} are small compared with those used to replicate synaptic noise.

For the model, all conductances and currents are reported in densities (i.e., per unit area). For comparison with experiments in which, for example, I_{stim} is not expressed per unit area, the model neuron can be assumed to have a surface area of about 300 μ m² (= 3 × 10⁻⁶ cm²). In other words, I_{stim} in μ A/cm² multiplied by 3 × 10⁻⁶ cm² × 10⁶ pA/ μ A gives I_{stim} in pA.

Dynamical analysis

Our modified Morris-Lecar model is ideally suited for dynamical analysis techniques because it comprises the minimum number of variables (dimensions) required to reproduce the phenomena of interest. Ideally, the system can be simplified to two dimensions, i.e., the interaction between a fast activation variable (e.g., V) and a slower recovery variable (e.g., w or z). That interaction can be visualized by plotting the fast variable against the slower variable to create a phase portrait. Nullclines represent areas in phase space where a given variable remains constant. How the nullclines intersect (i.e., whether the intersection is stable or unstable) determines whether the system evolves toward a fixed point or toward a limit cycle (i.e., subthreshold membrane potential or repetitive spiking, respectively). Stability of the fixed point can be determined by local stability analysis, which involves linearizing the nullclines in the vicinity of their intersection and finding the eigenvalues of the Jacobian matrix. This analysis leads to inequalities discussed in Fig. 5 (see Borisyuk and Rinzel 2005 for full derivations) and helps explain how voltage trajectories evolve toward or away from the fixed point, including the frequency of subthreshold MPOs.

The original Morris-Lecar model is two dimensional (2D). Our model is 3D because of the addition of slow adaptation. Because

adaptation develops slowly relative to the other variables, z (which controls adaptation; see preceding text) can be approximated as constant over some time window, thus allowing the model to be reduced from 3D to 2D; in other words, z is treated as a parameter and behavior is explained based on dynamical interaction between V and w. Initial analysis is based on this assumption. In the final two figures, however, slow changes in z are shown to be important for generating low-frequency oscillations. In this case, the system can still be approximated as 2D but with oscillations being explained by dynamical interaction between V and z (see RESULTS).

To determine the effects of certain parameters, the parameter of interest (e.g., $I_{\rm stim}$) can be continuously varied to determine its effects on the system's behavior, which will be reflected in the nullcline intersection. Of particular interest are bifurcations or abrupt transitions in the system's behavior, such as the transition between quiescence and repetitive spiking. See Rinzel and Ermentrout (1998) for a more detailed discussion of these methods in the context of neuronal excitability or Strogatz (1998) for an in-depth explanation.

RESULTS

Effects of shunting and adaptation on excitability in a modified Morris-Lecar model

Class 1 and 2 neurons initiate spikes through distinct dynamical mechanisms. Those dynamics represent competition between inward (depolarizing) and outward (hyperpolarizing) currents active at perithreshold potentials. In class 1 neurons, net current is inward at steady state. Sustained weak inward current allows the neuron to maintain slow repetitive spiking. This is manifested dynamically as a saddle-node on invariant circle (SNIC) bifurcation. In class 2 neurons, on the other hand, net current is outward at steady state. In this case, spike initiation requires that fast-activating inward current produces suprathreshold depolarization before slower-activating outward current becomes strongly activated (i.e., before net current becomes outward). This is manifested dynamically as a Hopf bifurcation. Importantly, class 2 neurons cannot maintain spiking below a critical rate lest slow-activating outward current overtake fast-activating inward current. For more detailed discussion of these points, see Izhikevich (2007) or Prescott et al. (2008).

A relative increase in outward current therefore encourages spike initiation through a Hopf bifurcation (class 2 excitability), whereas a relative increase in inward current encourages spike initiation through a SNIC bifurcation (class 1 excitability). Adaptation is caused by potassium currents the reversal potential of which is around -90 mV and, in the case of the M-type current $I_{\rm M}$, clearly contributes an outward current at perithreshold potentials. Similarly, shunting will produce an outward current at perithreshold potentials if its reversal potential is more hyperpolarized than threshold. Chance et al. (2002) calculated the conductance-weighted average of excitatory and inhibitory reversal potentials to be -57 mV, which is consistent with average membrane potentials reported by Destexhe and Paré (1999). Therefore shunting and adaptation both contribute outward current and are therefore predicted to encourage class 2 excitability. Decreased inward current (through cumulative sodium channel inactivation, for example) could cause a similar shift in net current with equivalent consequences for excitability (see following text).

To begin, we tested our theoretical prediction that increased outward current contributed by shunting and/or adaptation encourages class 2 excitability. First, we performed experiments in which in vivo-like conditions were replicated in acute brain slices using prolonged depolarizing current injections to activate adaptation with or without dynamic clamp to artificially increase membrane conductance (i.e., cause shunting) (Fig. 1*A, top*). Then,



FIG. 1. Shunting and adaptation convert neuronal excitability from class 1 to class 2. A, top: sample responses from a typical CA1 hippocampal pyramidal cell with and without shunting introduced artificially by dynamic clamp. Bottom: response from a modified Morris-Lecar model adjusted to qualitatively reproduce the experimentally observed response pattern. B: bifurcation diagrams were generated by varying stimulus intensity (I_{stim}) . The bifurcation represents the qualitative change in behavior from quiescence to repetitive spiking. Under control conditions (no adaptation or shunting; a), the model generated spikes through a saddle-node on invariant circle (SNIC) bifurcation, consistent with class 1 excitability. When shunting (b), adaptation (c), or both (d) were introduced, the model switched to generating spikes through a subcritical Hopf bifurcation, consistent with class 2 excitability. Shunting and adaptation both caused voltage at the bifurcation (V^*) to increase, which reflects the increased outward current contributed by shunting and adaptation at perithreshold potentials (see Fig. 2). For bifurcation analysis, activation of $I_{\rm M}$ (0 < z < 1) was held constant at the steady-state value of z measured from responses in A. C: I-V curves based on conditions in B. The steady-state I-V curve was nonmonotonic (i.e., it had a region of negative slope; see inset) under control conditions (a), whereas it was monotonic after adaptation and/or shunting were added (b-d). Instantaneous I-V curve was calculated as I_{Na} + I_{leak} while steady-state I-V curve was calculated as $I_{\text{Na}} + I_{\text{leak}} + I_{\text{K,dr}}$ (+ I_{M} if present).

starting with a modified Morris-Lecar model the parameters of which were set to values that give class 1 excitability, we added shunting and adaptation to reproduce the experimentally observed prohibition of repetitive spiking in the high-conductance state (Fig. 1*A, bottom*); the basis for this phenomenon has already been described in detail (Prescott et al. 2006) and results from nonlinearly increased activation of $I_{\rm M}$ at perithreshold potentials in the high-conductance state.

With model parameters thus established, we used bifurcation analysis to ascertain the spike-initiating mechanism under different conditions. Under control conditions (i.e., without shunting or adaptation), spikes were generated through a SNIC bifurcation (Fig. 1Ba), which is indicative of class 1 excitability. Consistent with the predicted effects of an increase in outward current (see preceding text), the spike-initiating mechanism switched to a subcritical Hopf bifurcation when shunting and/or adaptation were included in the model (Fig. 1B, b-d), thus demonstrating conversion to class 2 excitability. The switch in bifurcation mechanism was paralleled by a change in the steady-state I-V curve, from nonmonotonic under control conditions (Fig. 1Ca) to monotonic when shunting and/or adaptation were added (Fig. 1C, b-d). A nonmonotonic curve means there is a local maximum above which depolarization activates net inward current at steady state-this is the biophysical basis for spike initiation through a SNIC bifurcation. A monotonic curve has no local maximum, meaning fastactivating inward current must cause suprathreshold depolarization before slower-activating outward current causes net steady-state current to become outward-this is the biophysical basis for spike initiation through a Hopf bifurcation (see preceding text). The change in shape of the steady-state I-V curve is therefore consistent with the relative increase in outward current contributed by shunting and/or adaptation which causes net current at perithreshold potentials to change direction (see following text).

Effects of increased outward current on voltage threshold

Shunting and adaptation both caused a depolarizing shift in spike threshold (V^*) according to bifurcation analysis in Fig. 1B; threshold can be ascertained from voltage at the bifurcation. The shift is explained by the fact that inward current mediated by the fast sodium current I_{Na} must offset increased outward current contributed by shunting and adaptation; increased depolarization is required to activate I_{Na} more strongly to provide this increased inward current (Fig. 2A) and contributes to the depolarizing shift in V^* (Prescott et al. 2006). Importantly, the shift in V^* occurs in a steep region of the voltage-dependent activation curve for the delayed rectifier potassium current $I_{K,dr}$ (Fig. 2B) and for I_M (see following text). Consequently, a small change in V* allows dramatically increased activation of potassium currents at perithreshold potentials: this compounds the increase in outward current, exacerbates the depolarizing shift in V*, and causes the steadystate I-V curve to become monotonic (Fig. 2C).

Simulations therefore predicted that shunting and adaptation cause an increase in V^* . We therefore measured V^* in experimental data based on the voltage at which d^2V/dt^2 exceeded a cutoff value indicative of a spike. As predicted, both shunting and adaptation caused a depolarizing shift in V^* (Fig. 3, A and B). Furthermore, the experimentally measured shift in V^*



FIG. 2. Basis for and consequences of a depolarizing shift in voltage threshold (V^*). A: height of the local maximum of the instantaneous *I*-V curve was increased by the outward current contributed by shunting (\updownarrow). It was also shifted rightward (\leftrightarrow) because of the increased depolarization required to more strongly activate fast sodium current I_{Na} to counterbalance the increase in outward current; this contributes to the depolarizing shift in V^* and also allows for stronger subthreshold activation of the delayed rectifier potassium current $I_{K,dr}$ (see *B*) and the M-type potassium current I_M . B: $I_{K,dr}$ was only weakly activated at V^* under control conditions; however, because V^* sits in steep regions of its activation curve, modest changes in V^* (like in Fig. 1) allow for dramatically increased perithreshold activation of $I_{K,dr}$. \leftrightarrow , range of V^* identified in Fig. 1B. C: increased perithreshold activation of potassium currents causes net current to become outward at steady state, hence the "unbending" of the steady-state *I*-V curve, i.e., conversion from nonmonotonic to monotonic, as V^* is shifted.

occurred in a steep region of the activation curve for $I_{\rm K,dr}$, assuming typical parameters used to model Hodgkin-Huxley channels in hippocampal pyramidal neurons (Fig. 3*C*), and would therefore allow nonlinearly increased activation of $I_{\rm K,dr}$, consistent with the Morris-Lecar model reported in Fig. 2*B*. These data are therefore consistent with the postulated shift in balance of perithreshold currents that would account for the switch from class 1 to class 2 excitability.

Effects of shunting and adaptation on shape of the f-I curve

We then sought more direct evidence for a functional switch in excitability caused by shunting and adaptation. Because Hodgkin's original basis for classification was the shape of the f-I curve (see INTRODUCTION), we tested whether shunting and adaptation changed the f-I curve from continuous to discontinuous, consistent with a switch in excitability from class 1 to class 2.

Shunting had two effects on the *f-I* curve according to simulations: it shifted the curve rightward and increased the minimum sustainable firing rate (f_{\min}) to >0 spike/s, thus making the curve discontinuous (Fig. 4A). To determine effects of shunting on f_{\min} in experimental data while minimizing the



FIG. 3. Experimental evidence for a depolarizing shift in voltage threshold (V^*) . A: a 10-nS shunt produced a significant 2.3 \pm 0.5 (SE) mV depolarizing shift in V^* (P < 0.01, paired *t*-test, n = 6 cells). V^* was estimated as the voltage at which d^2V/dt^2 (which corresponds to rate of activation of I_{membrane}) exceeded a cutoff value 5× the root-mean-square noise in the baseline d^2V/dt^2 trace. Based on responses to I_{stim} 40 pA greater than rheobase, we measured V^* from the 2nd spike within each spike train because the 2nd spike occurs before adaptation develops, and its analysis is not confounded by initial membrane charging, as can occur with the 1st spike (modified from Prescott et al. 2006). B: adaptation also increased V^* measured, as in C, for sequential spikes within the initial burst. Data here are from a typical response and show a dramatic increase in V^* as adaptation develops. C: experimentally measured shifts in V^* (\leftrightarrow) sit within the steep region of the activation curve for $I_{\text{K,dr}}$ according to a typical Hodgkin-Huxley model used for hippocampal pyramidal cells (Traub and Miles 1991).

influence of adaptation, we measured instantaneous firing rate from the reciprocal of the first interspike interval or ISI and compared *f-I* curves in the low- and high-conductance states. Like in simulations, shunting shifted experimental *f-I* curves rightward and increased f_{\min} (Fig. 4*B*). Unlike in simulations, it is impossible to demonstrate experimentally that the neuron can spike at rates arbitrarily close to 0 spike/s (given the residual noise from ion channels, etc.), but, across all neurons tested, f_{\min} increased significantly from 3.5 ± 1.0 spike/s under control conditions to 16.4 ± 1.4 spike/s when a 10-nS shunt was applied to the neuron (P < 0.001, *t*-test, n = 6 cells; Fig. 4*C*).

To determine if adaptation caused a similar increase in $f_{\rm min}$, we measured instantaneous firing rate from the reciprocal of the last ISI within the initial burst (i.e., after development of adaptation). Once adapted, the same cell illustrated in Fig. 4*B* could not sustain spiking below ~20 spike/s regardless of $I_{\rm stim}$ (Fig. 4*D*). Across all neurons, adaptation significantly increased $f_{\rm min}$ in both the low- and high-conductance states to 16.2 ± 1.6 and 25.5 ± 1.6 spike/s, respectively (P < 0.005; Fig. 4*E*).

Thus shunting and tonic depolarization (which elicits adaptation) comparable to that experienced by neurons in vivo caused neuronal *f-I* curves to become discontinuous, consistent with the neuron switching from class 1 to class 2 excitability. By causing a switch to class 2 excitability, we predicted that shunting and adaptation encourage neurons to oscillate or resonate (i.e., respond more strongly to certain input frequencies), whereas those same neurons would not oscillate under control conditions when they are class 1 excitable.

Effects of shunting and adaptation on MPOs

We begin here by explaining the dynamical basis for the preceding prediction, i.e., why class 2 neurons oscillate whereas class 1 neurons do not. Class 1 neurons initiate their spikes on the basis of subthreshold inward current causing a SNIC bifurcation. This is reflected in the nonmonotonic steady-state *I*-*V* curve (Fig. 1*Ca*) and can be summarized by local stability analysis at the fixed point (see METHODS), which shows that $\partial I_{ss}/\partial V = 0$ at the *saddle-node* (Fig. 5*Aa*). The implications are that fast-activating inward current (I_{Na}) does not compete with slow-activating outward current ($I_{K,dr}$ or I_M) because the latter only starts to activate at suprathreshold voltages—this is why steady-state current is inward at perithreshold potentials and why the corresponding *I-V* curve has



FIG. 4. Shape of the *f-I* curve depends on stimulus conditions. *A*: *F-I* curves from model without adaptation. Shunting shifted the curve rightward and made it discontinuous, i.e., the shunted neuron could not sustain spiking below a minimum rate (f_{min}) of ~80 spike/s. A continuous *f-I* curve is consistent with class 1 excitability, whereas a discontinuous one is consistent with class 2 excitability. *B*: *F-I* curves from CA1 pyramidal neurons exhibited the same effects of shunting. Instantaneous firing rate (f_{inst}) was measured from the reciprocal of interspike intervals (ISIs); initial f_{inst} was calculated from the first ISI, which is relatively unaffected by slow adaptation. Sample responses highlight the shunting-induced increase in f_{min} , which was determined as initial f_{inst} for the minimum stimulus intensity eliciting ≥ 2 spikes (I_{min2}). Rectangles labeled *a* and *b* indicate responses shown in *D*. Arrow here and in *D* point to the subthreshold oscillation that follows the last spike of the initial burst; presence of an oscillation is consistent with class 2 excitability, whereas its absence is consistent with class 1 excitability (see Fig. 7). *C*: based on responses to I_{min2} , shunting caused a significant increase in f_{min} (P < 0.001, paired *t*-test, n = 6 cells). *D*: sample responses from same cell as in *B* show adaptation-induced increase in f_{min} . Instantaneous firing rate was measured from successive ISIs. I_{stim} was adjusted to give the same initial firing rate in the low- and high-conductance states (like in Fig. 1A); each graph shows different initial firing rates as indicated in *B*. Regardless of initial firing rate (i.e., *a* and *b* show equivalent results), f_{min} calculated from the last ISI (elicited by I_{min2}); with f_{min} calculated from the last ISI (elicited by $R > I_{min2}$) with f_{min} calculated from the last ISI (elicited by I_{min2}); that was true in both the low- and high-conductance states (P < 0.

a region of negative slope. In class 2 neurons, on the other hand, spike initiation occurs through a Hopf bifurcation because net current is outward at threshold, as reflected in the monotonic steady-state *I-V* curve (Fig. 1*C*, *b-d*). This means that I_{Na} must compete with $I_{\text{K,dr}}$ (or I_{M}) in a time-dependent manner. Subthreshold MPOs occur when inward current starts to activate but outward current catches up before a full spike occurs; this trajectory is manifested on the phase plane as spiraling around a stable focus $\left(-\frac{1}{C}\frac{\partial I_{\text{inst}}}{\partial V} < \frac{\phi_w}{\tau_w}\right)$ at the fixed point; Fig. 5*A*, *b* and *c*) (see also Hutcheon and Yarom 2000). Repetitive spiking occurs when that focus becomes unstable via a subcritical Hopf bifurcation $\left(-\frac{1}{C}\frac{\partial I_{\text{inst}}}{\partial V} > \frac{\phi_w}{\tau_w}\right)$.

By relating the generation of MPOs to the nullcline intersection, we can predict how conditions impact MPO frequency. MPO frequency reflects the rate of spiraling around the *focus*, which is reflected in the value of the complex component of the eigenvalue found by local stability analysis (Kaplan and Glass 1995). Equivalently, MPO frequency can be estimated from the phase plane: oscillations cannot occur when the V- and wnullclines intersect tangentially, but MPO frequency increases as the nullcline intersection becomes less acute (i.e., as the angle becomes less sharp) (Fig. 5A, middle row). The preceding is true for a given set of rate constants, but MPO frequency also depends on how rapidly outward current activates (controlled by $\phi_{\rm w}$ or $\tau_{\rm w}$) relative to instantaneous activation of inward current. Importantly, MPO frequency and f_{\min} are directly related insofar as MPO frequency is less than $f_{\min} + \Delta f$ (Fig. 5A, bottom row), where Δf accounts for subthreshold MPOs occurring in the bistable region of the bifurcation diagram (Fig. 5B).

Thus based on phase plane geometry, we know that class 2 neurons should oscillate whereas class 1 neurons should not.

Indeed the model did not exhibit subthreshold MPOs when depolarized to within a few millivolts of threshold under control conditions, when excitability was class 1 (Fig. 6A, black), but subthreshold MPOs were observed after the model was converted to class 2 excitability (Fig. 6A, gray). To show that MPOs resulted from the switch in excitability rather than being a specific consequence of shunting or adaptation, the model shown in Fig. 6A was converted to class 2 excitability by changing an unrelated parameter, β_m , which caused a depolarizing shift in the voltage-dependent activation curve for I_{Na} . Because greater depolarization was required to activate $I_{\rm Na}$, this parameter change caused a depolarizing shift in V* (like in Fig. 2A); as a result, spikes were generated through a Hopf bifurcation (bifurcation diagram not shown). Reducing the maximal sodium conductance (\bar{g}_{Na}) has a comparable effect (see following text).

If, instead of adjusting β_m , we added adaptation or shunting to the control model, the model exhibited subthreshold MPOs as predicted by its conversion to class 2 excitability (Fig. 6B). Furthermore, as predicted by local stability analysis (see corresponding phase planes in Fig. 5), the shunted neuron exhibited higher frequency MPOs than the adapted neuron given the parameters used (Fig. 6B). Also the amplitude (power) of MPOs was substantially less in the shunted neuron because low input resistance in the shunted neuron mitigated voltage changes. By stimulating our model with periodic inputs with different frequencies, we confirmed that class 2 models resonated at frequencies near their oscillation frequency, whereas the class 1 (control) model did not resonate, which is consistent with its inability to oscillate (Fig. 6C); both results are consistent with previous work (e.g., Izhikevich 2007).

We then compared these results with experimental data. Our recordings revealed subthreshold MPOs when CA1 pyramidal



FIG. 5. The dynamical basis for subthreshold membrane potential oscillations (MPOs). A: spike-initiating dynamics can be visualized on the phase plane in which model variables V and w are plotted relative to one another; nullclines represent everywhere in phase space where V or w do not change and are shown here for conditions at the bifurcation. In control (a), a spike cannot be generated until 2 fixed points (a saddle and a node) come together and are destroyed through a SNIC bifurcation, which occurs when the w- and Vnullclines meet tangentially. $\partial I_{ss}/\partial V = 0$ at the fixed point, which means net current is 0; in other words, spiking begins in a class 1 neuron when net current switches direction from outward to inward. With adaptation (b) or shunting (c) or both (not shown), the nullclines intersect at a single fixed point that switches from stable to unstable at the moment of the Hopf bifurcation. 1 $\partial I_{current} = \phi_{cur}$

 $-\frac{1}{C}\frac{\partial I_{\text{inst}}}{\partial V} = \frac{\phi_w}{\tau_w} \text{ at the fixed point, which means fast-activating inward current balances slower-activating outward current; in other words, spiking begins$

balances slower-activating outward current; in other words, spiking begins when activation of $I_{K,dr}$ cannot keep up with activation of I_{Na} . Nonetheless, $1 \ \partial I_{inst} \qquad \phi_w$

when $-\frac{1}{C} \frac{\partial I_{\text{inst}}}{\partial V} < \frac{\phi_{w}}{\tau_{w}}$, noisy voltage fluctuations can cause I_{Na} to begin to

activate before $I_{K,dr}$ catches up, which results in a depolarizing/hyperpolarizing sequence manifested as a subthreshold MPO. This is evident on the phase plane as spiralling around the fixed point or focus (not shown). Rate of spiralling (i.e., frequency of oscillations) can be inferred from how acutely the nullclines intersect and are less than $f_{min} + \Delta f$ (see following text). B: the bifurcation diagram (*bottom left*) and f-I curve (*top left*) are shown for conditions in *Ac. Right*: enlarged view of *left panels*. Notice the region of bistability, i.e., where the fixed point and limit cycle overlap. Because of this bistability, subthreshold MPOs can have a maximum frequency that is slightly higher than f_{min} (as indicated \rightarrow); we refer to this difference as Δf .

neurons were tonically depolarized. Oscillations were not necessarily obvious in the raw data, but power spectra showed a clear peak in the θ frequency range (Fig. 7A). In the lowconductance state, frequency at the peak of the power spectrum corresponded to the interval between doublet spikes in the sample traces. In the high-conductance state, amplitude of MPOs was reduced (i.e., power was reduced and spiking was virtually abolished), but there was still a clear peak in the power spectrum, which was shifted to a higher frequency than in the low-conductance state (Fig. 7A). Changes in MPO frequency and amplitude were consistent with the effects of shunting observed in simulations (see Fig. 6B). Similarly, MPO frequency increased as I_{stim} was increased (Fig. 7B), consistent with stronger stimulation eliciting stronger adaptation (i.e., larger outward current), which is again consistent with the model (simulation data not shown). As in our model, we confirmed that oscillating CA1 pyramidal neurons also resonated at θ frequency when stimulated with periodic input (Fig. 7*C*).

To determine whether CA1 pyramidal neurons could resonate without being tonically depolarized, we stimulated them with noisy current containing frequencies spanning the θ range (Fig. 7D, *inset*). This stimulation causes intermittent near-threshold depolarizations and can be used to reveal resonance the same way as periodic input (Schreiber et al. 2004). Using this protocol, we determined that CA1 pyramidal neurons in the low-conductance state that were not tonically depolarized did not resonate (Fig. 7D, black). However, when the same neuron was shunted, power was reduced at low frequencies and increased at high frequencies compared with the unshunted condition, which is consistent with the change in passive membrane properties (i.e., reduced input resistance and membrane time constant) but, more



FIG. 6. Occurrence and frequency of subthreshold MPOs in the model. A: just-subtreshold depolarization in the control model (black) did not elicit subthreshold MPOs, consistent with the inability of class 1 neurons to resonate. To demonstrate that resonance depends on excitability and is not a specific consequence of adaptation or shunting, we converted the model to class 2 excitability by changing β_m from -1.2 to 0 mV, which caused a depolarizing shift in V^* via changes in the activation curve for I_{Na} . This new model (gray) clearly exhibited MPOs. For simulations here and in B, low-amplitude noise was added as described in METHODS. B: as predicted by their effects on excitability, adding adaptation (black) or shunting (gray) to the control model caused it to oscillate. MPOs were faster in the shunted neuron than in the adapted neuron consistent with our explanation in Fig. 5. In both A and B, bottom traces show enlarged view of top traces. C: resonance was also tested by measuring impedance from responses to sine wave stimulation at different frequencies. As expected, the model neuron resonated at frequencies near its oscillation frequency shown in B.



FIG. 7. Occurrence and frequency of subthreshold MPOs in CA1 pyramidal neurons. A: traces show a typical response from a pyramidal neuron in the lowand high-conductance state. In both cases, like in Fig. 4, B and D, the initial burst was followed by a clear subthreshold MPO (\checkmark). Without shunting, the neuron occasionally fired doublet spikes (*) at an ISI related to the period of subthreshold MPOs (\rightarrow). Power spectra of perithreshold response (*left*) showed peaks in the θ frequency range; that peak shifted to a slightly higher frequency when the neuron was shunted, consistent with the effects of increased outward current (compare with Fig. 6B). \bigcirc , mean oscillation frequency and power (\pm SD) based on power spectral analysis of the 6 neurons analyzed. Oscillation frequency was significantly increased while power was significantly decreased by shunting (P < 0.01 and P < 0.05, respectively; paired *t*-test). Power spectra on right show lack of MPOs when neuron was not tonically depolarized. B: oscillation frequency also shifted as I_{stim} was increased, which is again consistent with the increased outward current caused by increased adaptation (see Fig. 5). C: resonance was also tested by measuring impedance from responses to sine wave stimulation at different frequencies. As expected, all neurons (n = 3) resonated at θ frequency when tonically depolarization (\bigcirc), but not when resting at -70 mV (\bullet). D: for these power spectra, the neuron was stimulated with large amplitude noise ($\sigma_{noise} = 40$ pA) that caused intermittent near-threshold depolarizations. The neuron resonated in the θ frequency range when in the high-conductance state (red) but not when in the low-conductance state. Male resonate at approximately the same frequency at which they oscillate in low-noise conditions, consistent with previous work (Erchova et al. 2004; Lampl and Yarom 1997). *Inset*: power spectrum of stimulus.

important here, the neuron exhibited resonance in the θ frequency range (Fig. 7*D*, red). Experimental data are therefore consistent with shunting and/or tonic depolarization converting CA1 pyramidal neurons from integrators to resonators.

Frequency of membrane potential oscillations

CA1 pyramidal neurons clearly oscillated in the θ frequency range (Fig. 7); however, our model neuron oscillated at significantly higher frequencies (Fig. 6). We therefore asked whether our model could produce lower frequency MPOs comparable to those observed experimentally. By reducing ϕ_w (which controls how rapidly $g_{K,dr}$ activates; see Eq. 2), MPO frequency was shifted down to the θ frequency range (Fig. 8A). However, reducing ϕ_{w} enough to produce θ frequency MPOs caused spikes to become unphysiologically wide (Fig. 8A, *inset*). This suggests that the process controlling θ frequency MPOs is significantly slower than the process controlling spike repolarization, and that the model must therefore include a third time scale. As alluded to in METHODS, $I_{\rm M}$ operates on a slower time scale than $I_{K,dr}$; hence, we attempted to generate θ frequency MPOs in our 3D model by adjusting the parameters controlling $I_{\rm M}$, most notably τ_z . As predicted, appropriately tuned $I_{\rm M}$ parameters resulted in θ frequency MPOs (Fig. 8B).

Time series in Fig. 8*C* illustrate how MPOs arise from the competition between inward and outward currents. During high-frequency MPOs, initial depolarization (which causes instantaneous activation of g_{Na}) is followed after a short delay by activation of $g_{K,dr}$, which causes hyperpolarization (Fig. 8*Ca*); although tonically activated, g_M does not vary on the time scale of these fast oscillations—this was the basis for approximating I_M as a constant for earlier analysis (see METHODS). During

low-frequency MPOs, on the other hand, initial slow depolarization is followed with virtually no delay by activation of $g_{K,dr}$, which means $g_{K,dr}$ does not provide the *delayed* outward current responsible for generating the oscillatory voltage change; instead, initial depolarization is followed by delayed activation of $g_{\rm M}$. In other words, slow voltage change allows enough time for $g_{\rm M}$ to vary, despite its slow kinetics, and thus to participate directly in generating MPOs. This has an important technical implication insofar as $I_{\rm M}$ cannot be approximated as remaining constant when explaining θ frequency MPOs. Nonetheless, generation of θ frequency MPOs can still be treated as a 2D problem (rather than a 3D one) because during slow oscillations, g_{Na} activates slowly and with kinetics similar to $g_{K,dr}$ (see Fig. 8*Cb*); accordingly, $I_{K,dr}$ can be approximated as an instantaneously varying offset in the competition between slow-activating I_{Na} and ultraslow-activating I_{M} .

The dynamics described above are also evident from phase plane analysis. Recall that w and z control activation of $I_{K,dr}$ and I_M , respectively. In the 2D model without I_M , shunting converted the intersection between the V- and w-nullclines from a saddle-node to a focus (Fig. 8Da), which is consistent with increased perithreshold activation of $I_{K,dr}$ (see Fig. 2); high-frequency MPOs result from spiraling around that focus (see Fig. 5). In the 3D model with I_M , the V- and w-nullclines intersected at a saddle-node despite adaptation (hence, no high-frequency MPOs), but the V- and z-nullclines intersected at a focus (Fig. 8Db), which is consistent with perithreshold activation of I_M ; θ frequency MPOs result from spiraling around this focus. Spiraling is slower on the V-z phase plane because of z's long time constant (see preceding text). These changes in phase plane geometry are paralleled by changes in the S. A. PRESCOTT, S. RATTÉ, Y. DE KONINCK, AND T. J. SEJNOWSKI



FIG. 8. Oscillation frequency in the model neuron. A: power spectra from modified model in which ϕ_w was reduced to 0.008, thus causing w to change more slowly relative to V (see Eq. 2). Under these conditions, the model neuron oscillated near 10 Hz when shunted (rather than near 100 Hz; see Fig. 6B), whereas the control neuron did not oscillate. However, reducing ϕ_w to 0.008 caused spikes to become unnaturally wide; *inset*: spike when $\phi_w = 0.008$ (black) for comparison with spike when $\phi_w = 0.25$ (gray). Other parameters were unchanged except $\gamma_w = 8 \text{ mV}$, $\bar{g}_{\text{K,dr}} = 30 \text{ mS/cm}^2$, $\tau_{\text{noise}} = 500 \text{ ms}$, and $\sigma_{\text{noise}} = 0.01 \ \mu\text{A/cm}^2$. B: alternatively, θ frequency oscillations could be generated by tuning the time constant for I_M (τ_z) to 400 ms. Other parameters were the same as in A except ϕ_w was returned to 0.25. In this model, adaptation caused ~8-Hz oscillations, whereas shunting continued to produce ~70-Hz oscillations. C: sample responses show the relative timing of changes in voltage (black), $g_{\text{K,dr}}$ (orange), and g_M (green). Recall that g_{Na} changes instantaneously with V. During high-frequency MPOs (a), activation of $g_{\text{K,dr}}$ kept up (i.e., activated instantaneously) with slow voltage changes. D: phase planes corresponding to conditions in B with nullclines shown for I_{stim} at the bifurcation. In the 2-dimensional (2D) model without I_M (a), the shunting-induced switch from class 1 to class 2 excitability was evident on the V-w plane plane based on the change in fixed point from saddle-node to focus. The model with adaptation (b) is 3D, and while the fixed point on the V-w plane remained a saddle-node, the fixed point on the V-z plane was a focus. In b, θ frequency oscillations arose from the interaction between I_{Na} and $ultraslow-activating <math>I_{\text{K,dr}}$ (visualized on the V-z plane) rather than through interaction between I_{Na} and slow-activating $I_{\text{K,dr}}$ (visualized on the V-w plane). E: correspondi

steady-state *I-V* curve insofar as perithrehsold activation of $I_{K,dr}$ or I_M both cause that curve to become monotonic (Fig. 8*E*).

To summarize, MPOs are generated when inward current competes with slower-activating outward current. We originally attributed MPOs to the competition between I_{Na} and $I_{K,dr}$, but subsequent analysis suggested that θ frequency MPOs arise from competition between I_{Na} and an outward current slower than $I_{K,dr}$, namely I_M . The competition between I_{Na} and I_M is the same as that between I_{Na} and $I_{K,dr}$: initial activation of inward current is followed by delayed activation of outward current-this is manifested as spiraling on the respective phase plane. Interestingly, our results show that $I_{\rm M}$ can, theoretically, contribute to oscillations in different ways: by competing directly with $I_{\rm Na}$ as described above (thus producing θ frequency MPOs) and also by providing a sustained outward current that shifts threshold and thus modulates the competition between I_{Na} and $I_{K,dr}$ (thus producing higher frequency MPOs; see Fig. 3).

Our experimental data from CA1 pyramidal neurons argue that $I_{\rm M}$ functioned uniquely through the first mechanism. First, power spectral analysis revealed MPOs in the θ frequency range but not at higher frequencies (see Fig. 7). Second, adaptation caused an increase in $f_{\rm min}$ to between 10 and 30 spike/s, depending on shunting (see Fig. 4); this is high enough to allow θ frequency MPOs (see Fig. 5) and is therefore consistent with $f_{\rm min}$ being determined by competition between $I_{\rm Na}$ and $I_{\rm M}$ but it is lower than would be predicted if $f_{\rm min}$ was determined by competition between $I_{\rm Na}$ and $I_{\rm K,dr}$. By extension, we would therefore argue that CA1 pyramidal neurons convert from class 1 to class 2 excitability primarily because of the outward current contributed by $I_{\rm M}$ rather than because of the outward current contributed by $I_{\rm K,dr}$ as initially hypothesized in Fig. 3. Importantly, voltage dependency of $I_{\rm M}$ is such that $I_{\rm M}$ can be activated at subthreshold voltages; by extension, a shift in V^* can significantly modulate the strength of perithreshold activation (Fig. 9A), which has already been shown to have important functional consequences (Prescott et al. 2006).

Effects of voltage threshold (V*) on strength of I_M

Variable activation of $I_{\rm M}$ (based on modulation of V^*) is important for explaining certain aspects of our experimental results. For one, CA1 pyramidal neurons spiked at low rates on initial depolarization from rest (Fig. 4, B and C); although $I_{\rm M}$ is slow to activate, it should be able prevent spiking below θ frequency (see preceding text). These data therefore suggest that $I_{\rm M}$ was not strongly activated on initial depolarization in nonshunted CA1 pyramidal neurons. This is consistent with the absence of resonance when nonshunted neurons were transiently depolarized to perithreshold voltages (Fig. 7D). However, nonshunted CA1 neurons clearly oscillated/resonated during sustained perithreshold depolarization (Fig. 7, A and C), which indicates that $I_{\rm M}$ did eventually activate under those conditions. Delayed activation of $I_{\rm M}$ is consistent with the observation that adaptation increased f_{\min} to $>\theta$ frequency (Fig. 4, D and E). One likely explanation for delayed activation



FIG. 9. Modulation of I_M via changes in V* and its implications for MPOs. A: voltage-dependent activation curve for I_M in our model (*left; original*: $\beta_z = -30$ mV and $\gamma_z = 5$ mV; *modified*: $\beta_z = -29$ mV and $\gamma_z = 2$ mV; $\tau_z = 400$ ms and $\overline{g}_M = 2$ mS/cm² in both) and based on measurements from CA1 pyramidal neurons (Wu et al. 2008) (*right*). A depolarizing shift in spike threshold (V*) allows for increased subthreshold activation of I_M . B: slow decrement in spike amplitude observed experimentally (*top*) suggests that sodium channels slowly inactivate during sustained depolarization. This was reproduced in the model

neuron by incorporating sodium channel inactivation implemented by multiplying \bar{g}_{Na} by h where $\alpha h/\alpha t = \frac{1}{2}$

= 0.67, $\beta_{\rm h} = -40$ mV, and $\gamma_{\rm h} = 8$ mV, and $\tau_{\rm h} = 1$ s. 33% inactivation of $g_{\rm Na}$ caused a ~15% drop in spike amplitude (*bottom*), which is similar to that observed experimentally (*top*). The model here used $\bar{g}_{\rm Na} = 24$ mS/cm², $\bar{g}_{\rm K,dr} = 30$ mS/cm², $\gamma_{\rm w} = 8$ mV, $\phi_{\rm w} = 0.25$, and the modified $I_{\rm M}$ parameters reported in *A*. For subsequent simulations, steady-state inactivation was implemented simply by reducing $\bar{g}_{\rm Na}$ by 33%. *C*: power spectra demonstrate that the model neuron described in *B* oscillated only when *V** was depolarized by shunting (pink) or by sodium channel inactivation (red); compare with lack of oscillations under control conditions (i.e., no inactivation and no shunting; blue) or when $I_{\rm M}$ was removed (green). *D*: phase plane showing intersection of *V*- and *z*-nullclines. As predicted, the fixed point was converted from a saddle-node to a focus by both shunting and sodium channel inactivation, consistent with the conditions under which the model oscillated in *C*. *E*: shunting and sodium channel inactivation caused increased perithreshold activation of $I_{\rm M}$, which caused the steady-state *I-V* curve to become monotonic, consistent with the change in phase plane geometry in *D*.

of $I_{\rm M}$ is that an even slower process, such as cumulative sodium channel inactivation that develops on the time scale of seconds (Fleidervish and Gutnick 1996), allows for increased activation of $I_{\rm M}$ when the neuron experiences sustained depolarization. Sodium channel inactivation was evident in our experimental data, for example, based on slow decrement in spike amplitude during sustained depolarization (Fig. 9B). Other results suggest that shunting allows for increased perithreshold activation of $I_{\rm M}$: transient depolarizations caused θ frequency resonance (Fig. 7D) and f_{\min} was $> \theta$ frequency on initial depolarization (Fig. 4, B and C) in shunted neurons. These data therefore suggest that shunting and cumulative sodium channel inactivation (or some other very slow process triggered by sustained depolarization) allow for increased perithreshold activation of $I_{\rm M}$ that causes net steady-state current to become outward, thus converting CA1 pyramidal neurons from class 1 to class 2 excitability and allowing them to oscillate at θ frequency.

To demonstrate the feasibility of this explanation, Fig. 9C shows how a model neuron with $I_{\rm M}$ oscillated at θ frequency when shunted or when sodium current was partially inacti-

vated, whereas the same neuron did not oscillate (because $I_{\rm M}$ was not strongly activated below V^*) under control conditions (i.e., no inactivation or shunting). Removing $I_{\rm M}$ from the model neuron prevented sodium channel inactivation (Fig. 9*C*, green curve) or shunting (data not shown) from causing oscillations, thus confirming that these two forms of modulation affected θ frequency MPOs by modulating activation of $I_{\rm M}$ rather than by modulating activation of $I_{\rm K,dr}$. Consistent with causing increased perithreshold activation of $I_{\rm M}$, shunting and sodium channel inactivation converted the intersection between the *V*- and *z*-nullclines from a saddle-node to a focus (Fig. 9*D*) and made the steady-state *I-V* curve monotonic (Fig. 9*E*).

 $\frac{n}{2}, h_{\infty}(V) = 1 -$

DISCUSSION

In this study, we used computational modeling and experiments in which in vivo-like conditions were recreated in an acute slice preparation to investigate whether CA1 pyramidal neurons behave as integrators or resonators, i.e., exhibit class 1 or 2 excitability according to Hodgkin's (1948) classification

 $\frac{1}{1+e^{(\beta_h-V)/\gamma_h}},\,\alpha_h$

scheme. Based on changes in voltage threshold, shape of the *f-I* curve, and ability to oscillate/resonate, our results demonstrate that although pyramidal neurons behave as integrators under typical in vitro conditions, those same neurons behave as resonators when shunted and/or tonically depolarized as is likely to occur in vivo (see INTRODUCTION). The change in coding strategy is fully accounted for by the relative increase in outward current caused by increased activation of $I_{\rm M}$, and the effects of that outward current on spike initiation.

The switch in excitability is interesting for several reasons. First, spike-initiating dynamics are typically thought of as an intrinsic property of the neuron, but results here indicate that spike initiation can be influenced by extrinsic factors like synaptic input (see also Steriade 2001). Second, the spikeinitiating mechanism is mutable rather than being a fixed property of the neuron as evidenced by its qualitative change from SNIC bifurcation to Hopf bifurcation. But despite the qualitative change in bifurcation mechanism, both f_{\min} and MPO frequency grow continuously from 0 Hz as the neuron transitions from class 1 to class 2 excitability (i.e., as net current at perithreshold potentials becomes more strongly outward). In fact, f_{\min} and MPO frequency are directly related insofar as MPO frequency is less than $f_{\min} + \Delta f$, where Δf accounts for subthreshold MPOs occurring in the bistable region of the bifurcation diagram (see RESULTS). Consistent with this, θ frequency (3–10 Hz) is less than our estimated value of $f_{\rm min}$ under in vivo conditions (~15-20 Hz). This relationship between f_{\min} and MPO frequency seems not to be broadly appreciated, but it suggests, for instance, that interneurons oscillating at γ frequency (30–80 Hz) must have even higher f_{\min} , which appears to be the case (Erisir et al. 1999; Tateno et al. 2004).

Several studies have documented the importance of intrinsic membrane properties for network synchronization (Di Garbo et al. 2007; Geisler et al. 2005; Pfeuty et al. 2003; Tateno and Robinson 2007). Pfeuty et al. (2003) specifically concluded that potassium currents promote synchrony, whereas persistent sodium current impedes synchrony, which is consistent with our results insofar as outward current encourages class 2 excitability, whereas inward current encourages class 1 excitability. Golomb et al. (2007) recently showed that increasing the sodium window current (which contributes inward current at perithreshold potentials) changed the bifurcation mechanism and prevented subthreshold voltage fluctuations, consistent with inward current switching the excitability of their model neuron to class 1. Hutcheon et al. (1996) also showed through modeling that shunting could encourage resonance, although they attributed that effect to a quantitative change in the membrane time constant rather than a qualitative change in spike-initiating mechanism. Our results are also consistent with work showing that adaptation mediated by $I_{\rm M}$ encourages class 2 excitability (Ermentrout et al. 2001), whereas cholinergic agonists, which block $I_{\rm M}$, have the opposite effect (Stiefel et al. 2008). Moreover, these results are consistent with reported effects of acetylcholine on low-frequency oscillations during slow-wave sleep (Steriade 2004). At first glance, our results appear to contradict Fernandez and White (2008), who showed that MPOs in entorhinal stellate cells were strongly attenuated by increased membrane conductance; in fact, our results are consistent insofar as shunting also attenuated MPOs in CA1 pyramidal cells and abolished spiking associated with those

MPOs (see Fig. 7*A*). One must consider that, to oscillate, CA1 pyramidal cells require a depolarizing shift in voltage threshold (caused by shunting, for example) to allow sufficient sub-threshold activation of $I_{\rm M}$ for the neuron to convert to class 2 excitability; entorhinal stellate cells, on the other hand, are likely class 2 under "control" conditions. Therefore although shunting is required for oscillations in the former cell type, it is not required for oscillations in the latter.

In the initial stages of this study, we hypothesized that shunting and adaptation (mediated by $I_{\rm M}$) allowed for increased activation of the delayed rectifier potassium current $I_{\rm K,dr}$ and that increased perithreshold activation of $I_{\rm K,dr}$ was responsible for making net steady-state current outward, thus causing excitability to become class 2. However, although increased perithreshold activation of $I_{K,dr}$ could theoretically contribute to the generation of high (e.g., γ) frequency oscillations, subsequent analysis (see Fig. 8) indicated that $I_{K,dr}$ did not have the kinetics required to generate low, θ frequency oscillations. This result is, perhaps, quite obvious. Nonetheless, results of that initial analysis provided the insight necessary to explain differential activation of $I_{\rm M}$ depending on operating conditions. Perithreshold activation of $I_{\rm M}$ can be increased by the same depolarizing shift in voltage threshold that could increase perithreshold activation of $I_{K,dr}$. Perithreshold activation of outward currents like $I_{\rm M}$ contribute to the shift in threshold, but, more important for understanding modulation of perithreshold activation of $I_{\rm M}$ are those processes that act on a faster or slower time scale than $I_{\rm M}$. Shunting and cumulative sodium channel inactivation caused by tonic depolarization are two such processes that cause a depolarizing shift in voltage threshold. Both are liable to be prominent under in vivo conditions but are modest under in vitro conditions, meaning $I_{\rm M}$ is liable to have a less pronounced effect in vitro than it would have in vivo. The result is that CA1 pyramidal neurons that function as integrators (class 1 excitable) in slice experiments may function as resonators (class 2 excitable) in the intact, awake brain. This is important given that neuron models are usually built based on parameters measured in vitro; such models may fail to reproduce, even qualitatively, important phenomena like oscillations and resonance. For one, the classic leaky integrate-and-fire model may not be ideal for modeling pyramidal cells, although variations such as the exponential integrate-and-fire model seem to capture some of the nonlinear dynamics at spike threshold (e.g., Fourcaud-Trocme et al. 2003).

To conclude, the dynamical mechanism underlying spike initiation can change qualitatively depending on conditions such as the level of background synaptic input. A switch in spike-initiating mechanism has several computationally important consequences and adds to a growing list of potential difficulties in extrapolating from in vitro data to explain neuronal operation in vivo. Nonetheless, in vivo-like conditions can be recreated in vitro and represent a useful approach for resolving potential discrepancies. These results remind us that vigilance is necessary when using a reductionist approach that relies on experimental conditions (e.g., brain slices) that do not fully replicate the complexities of the intact brain. Model building and carefully designed experiments are necessary to recognize and surmount these shortcomings.

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