

Measuring facial expressions by computer image analysis

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Abstract

Facial expressions provide an important behavioral measure for the study of emotion, cognitive processes, and social interaction. The Facial Action Coding System (Ekman & Friesen, 1978) is an objective method for quantifying facial movement in terms of component actions. We applied computer image analysis to the problem of automatically detecting facial actions in sequences of images. Three approaches were compared: holistic spatial analysis, explicit measurement of features such as wrinkles, and estimation of motion flow fields. The three methods were combined in a hybrid system that classified six upper facial actions with 91% accuracy. The hybrid system outperformed human nonexperts on this task and performed as well as highly trained experts. An automated system would make facial expression measurement more widely accessible as a research tool in behavioral science and investigations of the neural substrates of emotion.

Descriptors: Facial expression, Facial Action Coding System (FACS), Emotion, Computer image analysis

Facial expression measurement from video provides an indicator of emotion activity that is less intrusive than electroencephalography (EEG), electromyography, autonomic nervous system measurements and brain imaging. It is presently used in a variety of areas of behavioral research, including the study of emotion, social interaction, communication, anthropology, personality, and child development (for reviews, see Ekman, Huang, Sejnowski, & Hager, 1992; Ekman & Oster, 1979; Ekman & Rosenberg, 1997). Recent advances in computer vision and pattern recognition open up the possibility of automatic measurement of facial signals. An automated system would make facial expression measurement more widely accessible as a research tool in behavioral science and medicine and would provide alternative measures of visual stimuli and behavioral responses in psychophysiological investigations into the neural substrates of emotion and facial expressions.

Measurement of Facial Signals

The facial action coding system (FACS) (Ekman & Friesen, 1978) was developed to directly measure facial behavior.¹ Previous approaches to the study of facial expression measured information that observers *infer* from facial expressions. The difference between expression measurement and observer inference was reviewed by Ekman (1982a, 1982b). FACS was developed to address questions such as the differences in facial movement when people are telling the truth versus lying, the patterns of central nervous system activity that accompany different facial movements, and whether facial behavior predicts clinical improvement.

FACS allows precise specification of the morphology and the dynamics of facial movement. FACS was developed by determining from palpation, knowledge of anatomy, videotapes, and photographs how the contraction of each of the facial muscles changed the appearance of the face. Ekman and Friesen (1978) defined 46 action units (AUs) to correspond to each independent motion of the face. FACS is coded from video, and a trained human FACS coder decomposes an observed expression into the specific AUs that occurred and their duration, onset time, and offset time. More than 300 people worldwide have achieved intercoder agreement on FACS. A number of studies have appeared showing the rich variety of information that can be obtained by using FACS (see Ekman & Rosenberg, 1997, for a review).

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¹Electromyography also directly measures facial behavior, but it is obtrusive and not comprehensive.

Although FACS is a promising approach, a major impediment to its widespread use is the time required both to train human experts and to manually score the video tape. It takes over 100 hr of training to achieve minimal competency on FACS, and each minute of video tape takes approximately 1 hr to score. Automating FACS would make it more widely accessible as a research tool, and it would provide a good foundation for applications of automatic facial expression analysis in industry. An automated system would not only increase the speed of coding, it would also improve the reliability, precision, and temporal resolution of facial measurement.

Analysis of Facial Signals by Computer

Some success has been achieved for automatic detection of facial actions by tracking the positions of dots attached to the face (Himer, Schneider, Kost, Heimann, 1991; Kaiser & Wehrle, 1992). A system that detects facial actions from image sequences without requiring application of dots to the face would have much broader utility. Efforts have recently turned to measuring facial actions by image processing of video sequences (Bartlett et al., 1996; Cohn, Zlochower, Lien, Wu, & Kanade, in press; Lien, 1998). Here, we explore and compare methods for classifying facial actions in image sequence of faces.²

Recent advances have been made in computer vision for automatic recognition of facial expressions in images. The approaches that have been explored include analysis of facial motion (Essa & Pentland, 1997; Mase, 1991; Rosenblum, Yacoob, & Davis, 1996; Yacoob & Davis, 1994), measurements of the shapes of facial features and their spatial arrangements (Lanitis, Taylor, & Cootes, 1997), holistic spatial pattern analysis using techniques based on principal components analysis (PCA) (Cottrell & Metcalfe, 1991; Lanitis et al., 1997; Padgett & Cottrell, 1997), and methods for relating face images to physical models of the facial skin and musculature (Essa & Pentland, 1997; Li, Roivainen, & Forcheimer, 1993; Mase, 1991; Terzopoulos & Waters, 1993). These systems demonstrate approaches to face image analysis that are applicable to the present goals, but the systems themselves are of limited use for behavioral and psychophysiological research.

Facial action codes versus emotion categories. Most of the computer vision systems for recognizing facial expressions attempt to classify expressions into a few broad categories of emotion, such as happy, sad, or surprised. The evidence for seven universal facial expressions (see Ekman, 1989, for a review) does not imply that these emotion categories are sufficient to describe all facial expressions (Hager & Ekman, 1995). If automated facial measurement were to be constructed simply in terms of seven elementary emotional categories, much important information would be lost: blends of two emotions, variations within an emotional category (e.g., vengeance vs. resentment), variations in intensity (e.g., annoyance vs. fury), conversational signals, and idiosyncratic facial movements.

Systems that only produced emotion category labels also could not be used in investigations of facial behavior itself. Several computer vision systems explicitly parameterize facial movement (Yacoob & Davis, 1994) and relate facial movements to the underlying facial musculature (Essa & Pentland, 1997; Mase, 1991), but these descriptions are not readily interpretable in terms of facial action codes. It is unknown whether these descriptions are

sufficient for describing the full range of facial behavior, and the relationship between these measures and internal state has not been established. A large body of empirical data already exists demonstrating the relationship of facial action codes to emotions, emotion intensity, variations, blends, and conversational signals.

Analysis of facial motion. The majority of the computer vision work on facial expression recognition has focused on facial motion analysis through optic flow estimation. If the tissues and muscles are similar between different people, the motions that result from facial action should be similar, independent of surface level differences between faces. In an early exploration of facial expression recognition, Mase (1991) used optic flow to estimate the activity in 12 of the 44 facial muscles. For each muscle he defined a window in the face image and an axis along which each muscle expands and contracts. The mean similarity of the flow vectors inside the window to this axis provided a coarse estimate of the activity of the muscle. Yacoob and Davis (1994) constructed a midlevel representation of facial motion from the optic flow output, which consisted of such descriptions as *right mouth corner raises*. The midlevel representation was then classified into one of six facial expressions using a set of heuristic rules. Rosenblum et al. (1996) expanded this work to analyze facial expressions using the full temporal profile of the expression, from initiation to apex and then to relaxation. They trained radial basis function neural networks to estimate the stage of an expression from a facial motion description, and constructed separate networks for each expression. Radial basis functions approximate nonlinear mappings by Gaussian interpolation of examples and are well suited to modeling systems with smooth transitions between states. Beymer, Shashua, and Poggio (1993) trained radial basis function neural networks to learn the transformation from optic flow fields to pose and expression coordinates and from pose and expression coordinates back to optic flow fields. The estimated optic flow fields could be used to synthesize new poses or expressions from an example image by image warping techniques. The work most closely related to the approach we have taken here is that of Cohn et al. (in press), who are building a system to classify facial actions by facial feature point tracking. Over 40 points were manually located in the initial face image, and the displacements of these feature points were estimated by optic flow. Discriminant functions classified the displacements into three action classes in the brow region, three in the eye region, and nine in the mouth region.

Model-based techniques. Several facial expression recognition systems have employed explicit physical models of the face (Essa & Pentland, 1997; Li et al., 1993; Mase, 1991; Terzopoulos & Waters, 1993). Essa and Pentland (1997) extended a detailed anatomical and physical model of the face developed by Terzopoulos and Waters (1993) and applied it to both recognizing and synthesizing facial expressions. The model consisted of a geometric mesh with 44 facial muscles, their points of attachment to the skin, and the elastic properties of the skin. Images of faces were mapped onto the physical model by image warping based on the locations of six points on the face. Motion estimates from optic flow were refined by the physical model in a recursive estimation-and-control framework, and the estimated forces were used to classify the facial expressions. In a model-based system, classification accuracy is limited by the validity of the model. There are numerous factors that influence the motion of the skin following muscle contraction, and it would be difficult to accurately account for all of them in a deterministic model. Here, we take a neural network

²A brief report of this work was published by Bartlett et al. (1996).



Figure 1. Example action sequence from the database. The example shows a subject performing AU 1 starting from a neutral expression and ending with a high-magnitude action.

approach to image analysis in which facial action classes are learned directly from example image sequences of the actions, bypassing the physical model.

Feature-based approaches. One of the earliest approaches to recognizing facial identity in images was based on a set of feature measurements such as nose length, chin shape, and distance between the eyes (Brunelli & Poggio, 1993; Kanade, 1977). Lanitis et al. (1997) recognized identity, gender, and facial expressions by measuring shapes and spatial relationships of a set of facial features using a flexible face model. An advantage of the feature-based approach is that it drastically reduces the number of input dimensions. A disadvantage is that the specific image features relevant to the classification may not be known in advance, and vital information may be lost when compressing the image into a limited set of features. Moreover, holistic gray-level information appears to play an important role on human face processing (Bruce, 1988; Bruce, Hancock, & Burton, 1998).

Holistic analysis. The alternative to feature-based image analysis, holistic analysis, emphasizes preserving the original images as much as possible and allowing the classifier to discover the relevant features in the images (Movellan, 1994). An example of this approach is template matching. Templates capture information about configuration and shape that can be difficult to parameterize. In related neural network approaches to image analysis, the physical properties relevant to the classification need not be specified in advance and can be learned from the statistics of the image set, which is particularly useful when the specific features relevant to the classification are unknown (Valentin, Abdi, O'Toole, & Cottrell, 1994).

One holistic spatial representation is based on the principal components of the image pixels (Cottrell & Fleming, 1990; Turk & Pentland, 1991). PCA finds an orthogonal set of dimensions that account for the principal directions of variability in the data set. The component axes are template images that can resemble ghost-like faces, which have been labeled *holons* (Cottrell & Flemming, 1990) and *eigenfaces* (Turk & Pentland, 1991). A low-dimensional representation of the face images with minimum reconstruction error is obtained by projecting the images onto the first few principal component axes. PCA has been applied successfully to recognizing both facial identity (Cottrell & Fleming, 1990; Turk & Pentland, 1991) and facial expressions (Bartlett et al., 1996; Cottrell & Metcalfe, 1991; Padgett & Cottrell, 1997). Another holistic spatial representation is obtained by a class-specific linear projection of the image pixels (Belhumeur, Hespanha, & Kriegman, 1997). Accurate alignment of the faces is critical to the success of such image-based approaches. Feature-based and template-based

methods need not be mutually exclusive. Lanitis et al. (1997) recognized identity, gender, and facial expressions by measuring shapes and spatial relationships of a set of facial features using a flexible face model. Performance improved by augmenting a set of feature measurements with parameters containing information about modes of variation in gray-level images based on PCA.

Automating FACS

We explored three different methods for classifying facial actions that were suited to detecting different kinds of image cues: holistic spatial analysis based on principal components, a feature-based approach that measures facial wrinkles and eye opening, and facial motion analysis based on template matching of optic flow fields. The performances of the three systems were compared and then combined into a single system that pools their strengths. One benchmark for the performances of the automated systems was provided by the ability of naive human subjects to classify the same images. A second benchmark was provided by the agreement rates of expert coders on these images.

Methods

Image database. We collected a database of image sequences of subjects performing specified facial actions. The full database contained over 1,100 sequences containing over 150 distinct actions or action combinations. The image database was obtained from 24 Caucasian subjects, 12 males and 12 females. Their ages ranged from 19 to 61 years (median = 30 years). Thirteen were experienced FACS coders, eight had some FACS training, and three were naive. Each image sequence consisted of six frames, beginning with a neutral expression and ending with a high-magnitude muscle contraction (Figure 1). The database therefore contained examples of the facial actions at low, medium, and high magnitude.³ Trained FACS experts provided demonstrations and instructions to subjects on how to perform each action. The selection of images was based on stop motion video coded by three experienced FACS coders certified with high intercoder reliability. The criterion for acceptance of images was that the requested action and only the requested action was present.

For this investigation, we used data from 20 subjects and attempted to classify the six individual upper face actions illustrated in Figure 2. This set of actions was chosen because the facial actions in the upper face comprise a relatively independent subset of facial actions; facial actions in the upper face have little influence on facial motion in the lower face, and vice versa (Ekman &

³The term *magnitude* replaces the term *intensity* used in FACS to avoid confusion with image intensity.



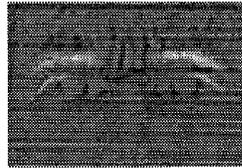
AU 1. Inner Brow Raiser

Central frontalis muscle contracts.
Inner corners of brows raise up,
In some subjects, brows make inverted V.
Wrinkles in center of forehead, slight U-shape.



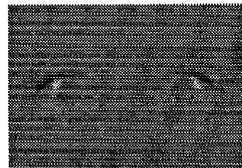
AU 2. Outer Brow Raiser

Lateral frontalis muscle contracts.
Pulls lateral portion of the eyebrows upward, producing 
Wrinkles on sides of forehead.
Lateral portion of eye cover fold stretches upwards.



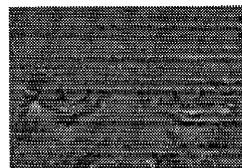
AU 4. Brow Lower

Brows lower and / or draw together.
Produces deep vertical and / or 45 degree wrinkles between brows.
Pushes eye cover fold downwards and may narrow eye opening.
May also produce horizontal wrinkles at root of nose and oblique bulge over medial corner of brow.



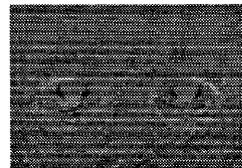
AU 5. Upper Lid Raiser

Upper lid retracts, widens eye opening.
Decreases visibility of upper lid.
Increases exposure of sclera above the iris, and on the sides.
Eyeballs appear to protrude.



AU 6. Cheek Raiser

Orbital muscles around the eye contract
May cause crows feet to appear or deepen.
Makes infraorbital furrow evident - straight or crescent shape.
Causes bagging or wrinkling of the skin below the eye.
Changes under eye are lower on face than AU 7



AU 7. Lid Tightener

Tightens eyelids, narrowing the eye opening.
More apparent in lower lid. Lower lid covers more sclera and iris.
Lower lid straightens or medial portion slightly inverts. 
Bulge appears in lower lid and lower eyelid furrow may deepen
Can produce single "crow's toe," not crows feet as in AU 6.

Figure 2. Examples of the six actions (AU 1–6) used in this study. Left: Cropped image of the action at highest magnitude. Right: Difference image obtained by subtracting the neutral image (Frame 1 of the sequence). Action unit description adapted from Ekman and Friesen (1978).

Friesen, 1978). Most subjects were able to perform only a subset of the actions without interference from other facial muscles. Each subject performed a mean of four actions. The dataset therefore contained, aside from the neutral frame, a total of 400 images of facial actions (20 subjects \times 4 actions \times 5 frames per action). Nine subjects performed AU 1, 10 performed AU 2, 18 performed AU 4, all 20 performed AU 5, 5 performed AU 6, and 18 performed AU 7.

Faces were aligned, cropped, and scaled based on the locations of two points in the first frame of each sequence. The two points were indicated by a single mouse click at the center of each eye. All other procedures were fully automated. Accurate image regis-

tration is critical for principal components based approaches. The variance in assigned eye location using this procedure was 0.4 pixels in the 640- \times 480-pixel images.

The eye positions from Frame 1 were used to crop all subsequent frames and to scale the faces to 45 pixels between the eyes. The images were rotated in the plane so that the eyes were horizontal, and the luminance brightness values were linearly rescaled to [0, 255]. The images were cropped to contain only the upper half of the face, as shown in Figure 2. The final images contained 66 \times 96 pixels. Difference images, which were used in the holistic analysis, were obtained by subtracting the neutral expression frame (the first frame in each sequence) from the five subsequent frames.

Advantages of difference images include robustness to changes in illumination, removal of surface variations in facial appearance, and emphasis of the dynamic aspects of the image sequence (Movellan, 1995).

Because faces tend to be asymmetric and the contractions of facial muscles are also frequently asymmetric, we generated additional training data by reflecting each image about the vertical axis. Mirror reversed images of test subjects were never included in the training set, so the classifiers had no access to information about reflected test images either during parameter estimation or classification. The reflected images were not assumed to be independent of their originals and were not counted in the N for statistical comparisons. All 400 difference images in the data set were asymmetric. The reflected images differed from their originals in 6,125 of the 6,336 pixels on average, and the mean magnitude of the difference was 5.36. Images differed between individuals in an average of 6,179 pixels, and the mean magnitude of the difference between individuals was 7.17. The symmetry of the training set also ensured that the classifiers had no asymmetric bias.

Holistic spatial analysis. We first evaluated the ability of a back-propagation network to classify facial actions given principal components of gray-level images as input. This approach is based on the work of Cottrell and Metcalfe (1991) and Turk and Pentland (1991); the primary distinction is that we performed PCA on the data set of difference images. The remaining variation in the data set of difference images was that due to the facial dynamics. Each of the 800 difference images was converted to a vector by concatenating the rows of pixel intensities. The principal component axes of the difference image data were then calculated by finding

the eigenvectors of the pixelwise covariance matrix. The axes were ordered by the magnitude of the corresponding eigenvalue. Figure 3 shows the first 12 principal components of the difference images.

The principal component representation consisted of a set of coefficients obtained by projecting each difference image onto the component axes. These coefficients comprised the input to a two-layer neural network with 10 hidden units and six output units, one per action. The network was a feed-forward one, with each unit connected to all of the units in the layer above (see Haykin, 1994). The activities of the hidden and output units were calculated sequentially as the weighted sum of their inputs, passed through a sigmoidal hyperbolic tangent transfer function. The network was trained by back-propagation of error to output a 1 for the appropriate action and zeros everywhere else, using conjugate gradient descent on the summed squared error. Stopping criterion was the inflection point in the mean test error. The output unit with the highest activity determined the classification.

Feature measurement. Four of the upper face actions produce wrinkles in distinct locations on the face, and the remaining two alter the amount of visible sclera. We applied a method developed by Jan Larsen (Bartlett et al., 1996) for measuring changes in facial wrinkling and eye opening. The feature measurements were carried out on 360×240 -pixel images. Facial wrinkles were measured at the four facial positions shown in Figure 4a, which were located in the image automatically from the eye position information. These image locations were selected for detecting wrinkles produced by AUs 1, 2, 4, and 6. At each location, mean pixel intensities of a five-pixel-wide segment were extracted and then

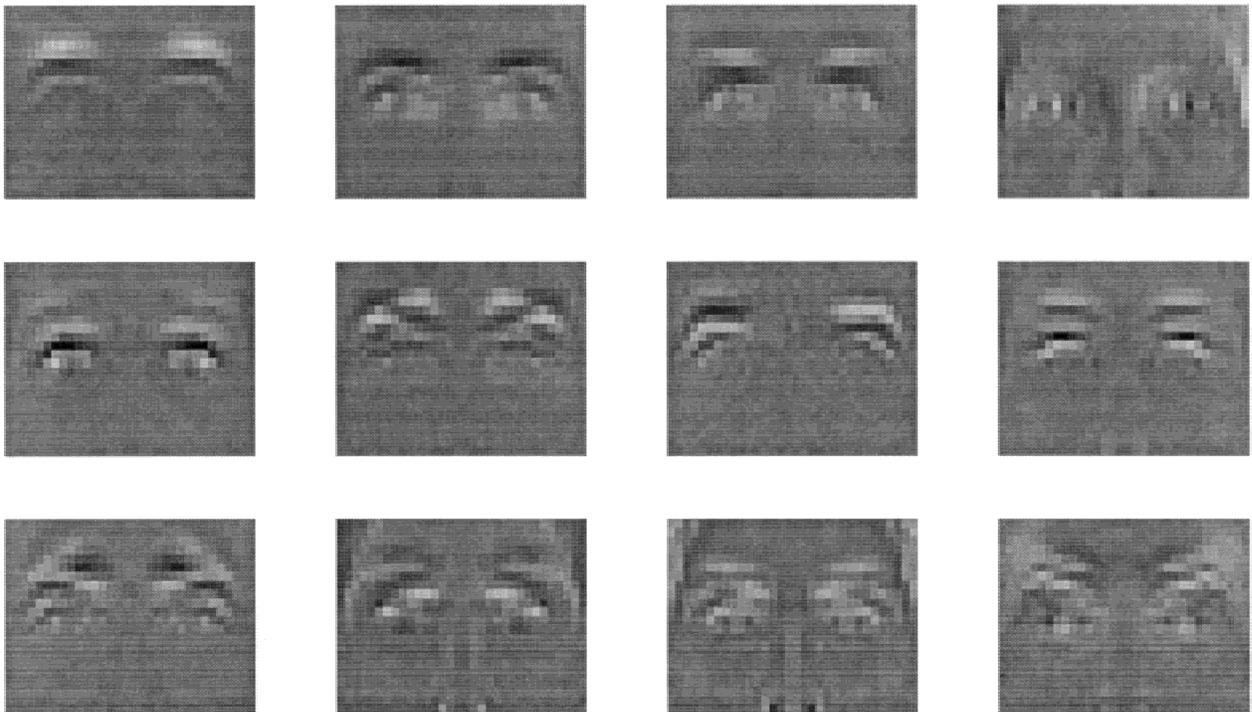


Figure 3. First 12 principal components of the dataset of difference images, ordered left to right, top to bottom. The first component appears to code for vertical brow position. The sixth component axis appears to differentiate between AU 1, raising the inner corners of the brow, and AU 2, raising the lateral portions of the brows. Component 7 appears to be an axis of left–right asymmetry in the lateral brow movement, and component 5 appears to be an eye opening axis.

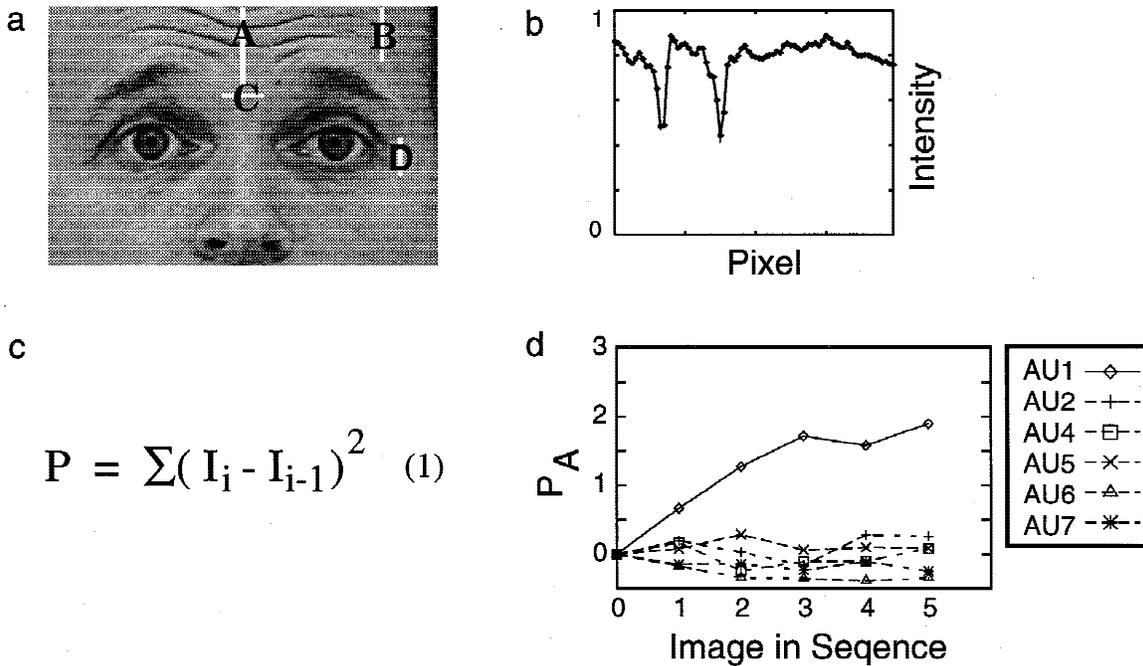


Figure 4. a. Wrinkling was measured at four image locations, A–D. b. Smoothed pixel intensities along the line labeled A. c. The wrinkle measure, P . I_i is the intensity of the i th pixel of the segment. Pixel differences approximate the derivative (Jain, Kasturi, & Schunk, 1995). d. P measured at image location A for one subject performing each of the six actions.

smoothed lengthwise by a median filter. Figure 4b shows the smoothed pixel intensities along the image segment labeled A. The pixel intensities drop sharply at the two major wrinkles.

We chose as a measure of facial wrinkling the sum squared derivative of the pixel intensities along the segment. This value is estimated by P (Figure 4c.) This measure is sensitive to both the deepening of existing wrinkles and the addition of new wrinkles. To control for permanent wrinkles, P values for the neutral image were subtracted. Figure 4d shows P values along line segment A, for a subject performing each of the six actions. P remains at zero except for AU 1, for which it increases as action magnitude increases. Only AU 1 produces wrinkles in the center of the forehead.

For detecting and discriminating AUs 5 and 7, we defined an eye opening measure as the area of visible sclera lateral to the iris. This area was found by starting at the pupil and searching laterally for connected rows of pixels above threshold. Again, differences from baseline were measured. A three-layer neural network was trained to classify each image from the five feature measures, consisting of the wrinkle feature measured at four locations and the eye opening measure. The network had 15 hidden units and 6 output units.

Optic flow. Local estimates of motion in the direction of the image gradient were obtained by an algorithm based on the brightness constraint equation (Horn & Schunk, 1981):

$$\frac{dI(x, y, t)}{dt} = \frac{\partial x}{\partial t} \frac{\partial I(x, y, t)}{\partial x} + \frac{\partial y}{\partial t} \frac{\partial I(x, y, t)}{\partial y} + \frac{\partial I(x, y, t)}{\partial t} = 0. \quad (2)$$

This equation assumes that there is no overall gain or loss of brightness in the image I over time, and any changes in brightness

can be accounted for by shifts in spatial position. The local image velocities, $v_x = \partial x / \partial t$ and $v_y = \partial y / \partial t$, are defined in terms of the spatial and temporal gradients of the image, $\partial I / \partial x$, $\partial I / \partial y$, and $\partial I / \partial t$.

Optic flow was estimated between image pairs, a given frame in an action sequence, t_i , and the neutral frame, t_0 . Images were smoothed by a 5×5 Gaussian kernel. Estimates of the spatial gradients, ΔI_x and ΔI_y , were obtained with horizontal and vertical Sobel edge filters. The temporal gradient was estimated by $\Delta I_t = I(x, y, t_i) - I(x, y, t_0)$. Local estimates of image velocity in the direction of the gradient were obtained by $v_x = \Delta I_t / \Delta I_x$ and $v_y = \Delta I_t / \Delta I_y$.

Gradient-based techniques for estimating optic flow give reliable estimates only at points where the gradient is high (i.e., at moving edges). Velocity estimates were set to zero at locations at which the total edge measure $r = \Delta I_x^2 + \Delta I_y^2$ was beneath a threshold of 0.2. An example flow field is shown in Figure 5. One of the advantages of this simple local estimate of flow was speed. It took 0.13 s on a 120-MHz Pentium processor to compute one flow field.

The flows fields were classified by a template matching procedure. A weighted template for each of the actions was calculated from the training images as the mean flow field at medium action magnitude (Frame 4 of the sequence). Novel flow patterns, f^n , were compared to the template f^t by the correlational similarity measure S :

$$S(f^n, f^t) = \frac{\sum_i f_i^n \cdot f_i^t}{\sqrt{\sum_i f_i^n \cdot f_i^n} \sqrt{\sum_i f_i^t \cdot f_i^t}}, \quad (3)$$

where i indexes image location. $S(f^n, f^t)$ is the cosine of the angle between the two flow vectors.

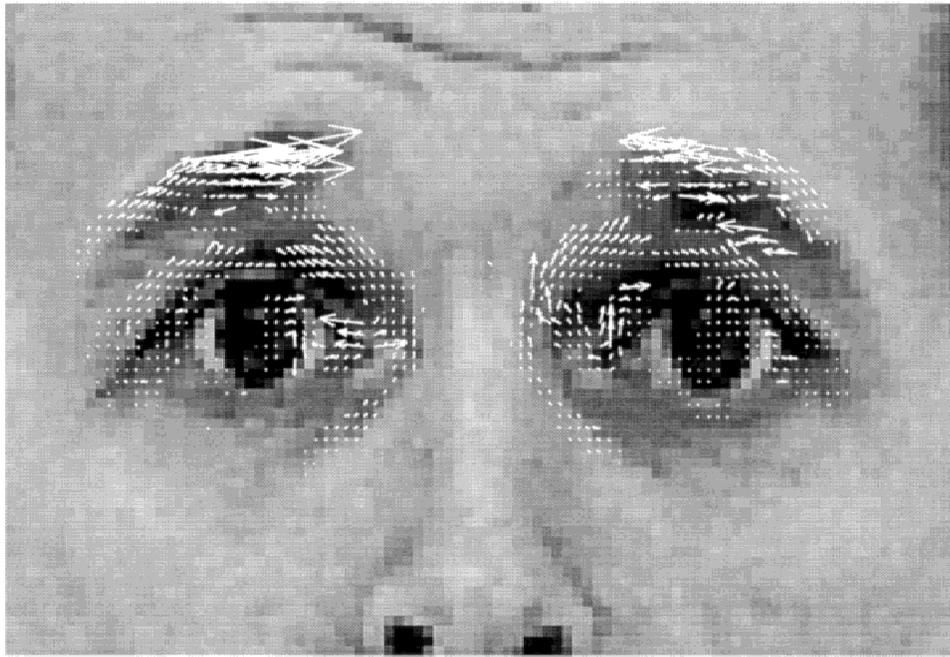


Figure 5. Example flow field of a subject performing AU 1, inner brow raiser. The flow vector at each image location is plotted as an arrow with length proportional to the local estimate of velocity.

Naive human subjects. Naive subjects were nine adult volunteers with no prior knowledge of facial expression measurement. Subjects were provided with a guide sheet similar to Figure 2, which contained an example image of each of the six actions along with a written description of each action and a list of image cues for detecting and discriminating the actions from Ekman and Friesen (1978). Each subject was given a training session in which the facial actions were described and demonstrated, and the image cues listed on the guide sheet were reviewed and indicated on the example images. The subjects kept the guide sheet as a reference during the task.

Face images were cropped and scaled identically to how they had been for the automated systems, with 45 pixels between the eyes, and printed using a high-resolution HP Laserjet 4si printer with 600 dpi. Because the automated systems had information about the test image and the neutral image when making a classification, face images were presented to the human subjects in pairs, with the neutral image and the test image presented side by side. Subjects were instructed to compare the test image with the neutral image and decide which of the actions the subject had performed in the test image. Subjects were given a practice session with feedback consisting of one example of each action at high magnitude. Neither the practice face nor the reference face was used for testing. The task contained 96 image pairs, consisting of low-, medium-, and high-magnitude examples of the six actions from six different faces, three male and three female. Subjects were allowed to take as much time as they needed to perform the task, which ranged from 30 min to 1 hr.

Expert coders. Expert subjects were four certified FACS coders. The task was identical to the naive subject task with the following exceptions. Expert subjects were not given a guide sheet or additional training, and the complete face was visible, as it would normally be during FACS scoring. One hundred fourteen image

pairs were presented, consisting of low-, medium-, and high-magnitude examples of the six actions from seven faces. Time to complete the task ranged from 20 min to 1 hr and 15 min.

Results

Generalization to novel faces was tested using leave-one-out cross-validation (Tukey, 1958). This procedure makes maximal use of the available data for estimating parameters. System parameters were estimated 20 times, each time using images from 19 subjects for training and reserving all of the images from one subject, including the reflected images, for testing. The system parameters were deleted and reestimated for each test. Mean classification performance across all test images in the 20 cross-validation runs was then calculated.

With this procedure, there were 800 test images, containing low-, medium-, and high-magnitude examples of the facial actions. The systems classified the test images one frame at a time, without reference to previous outputs. Figure 6 is a plot of the overall mean performances of the classifiers on novel faces. Performances by facial action are the diagonal entries in the confusion matrices in Tables 1 and 2.

Holistic spatial analysis. Classification performance was evaluated for two scales of difference images, 66×96 and 22×32 , and for five quantities of principal components in the network input: 10, 25, 50, 100, and 200. There was a trade-off between increasing the amount of information in the input and increasing the number of free parameters to be estimated. The higher principal components may also include more information on between-subject variations. We obtained the best performance of 88.6% using the first 50 principal components of the 22×32 difference images.

The holistic system with 50 principal components had 580 parameters, and our training set in a given training run contained

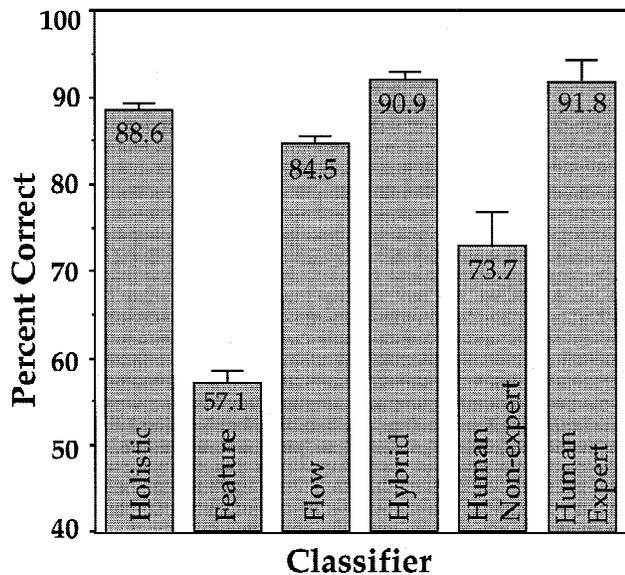


Figure 6. Performance comparisons for generalization to novel subjects. Values are percent correct across all test images. Error bars are 1 *SD* of the estimate of the success rate in a Bernoulli distribution. Human results were prorated by action and action magnitude to match the proportions in the complete image set.

on average 760 images. Overparameterization is a risk with such high dimensional networks. Performance for generalization to novel faces provided a measure of how well the system performed the general class discrimination, as opposed to finding a trivial solution that minimized the error for the training samples without learning the class discrimination.

The performance of 88.6% is substantially higher than the 70% performance reported by Padgett and Cottrell (1997) for facial expression classification using full-face eigenfaces. The success of the present system could be attributable to reduced variability due to the use of difference images or to the smaller original image size, so that 50 principal components accounted for a greater percentage of the variability. In addition, we employed a region of interest analysis, consisting of half of the face image, which is similar to the eigenfeature approach that gave Padgett and Cottrell better performance.

Table 1. Confusion Matrix for Naive (*Nv*) and Expert (*Ex*) Human Subjects

Action unit	Responses											
	AU 1		AU 2		AU 4		AU 5		AU 6		AU 7	
	<i>Nv</i>	<i>Ex</i>										
AU 1	.84	.99	.08	.00	.03	.00	.02	.00	.02	.00	.02	.01
AU 2	.12	.04	.83	.93	.00	.00	.03	.00	.01	.00	.00	.02
AU 4	.03	.00	.03	.01	.88	.96	.01	.00	.02	.00	.03	.02
AU 5	.09	.00	.20	.01	.00	.01	.64	.98	.03	.00	.03	.01
AU 6	.04	.00	.03	.01	.04	.00	.00	.00	.55	.41	.34	.58
AU 7	.00	.00	.04	.00	.05	.02	.00	.00	.26	.09	.65	.89

Note: Values are the percent occurrence of each response for a given action.

Feature measurement. The performance of the feature-based classifier on novel faces was lower than that of the other methods, at 57% correct. Normalization of the feature measures with Z scores did not improve performance. The classifier was most accurate for the two actions that involved changes in eye opening, AU 5 and AU 7, at 74% and 62% correct, respectively. The poor performance for novel faces may be attributable to the differences in facial wrinkling patterns between subjects depending on skin elasticity, facial structure, and fat stores. The feature-based classifier performed well for new images of a face used for training, with classification accuracy of 85.3%.

Optic flow. Template matching of motion flow fields classified the facial actions with 84.5% accuracy for novel subjects. The performance of the motion-based classifier was similar to that of the holistic classifier, giving highest accuracy for AUs 2, 4, 5, and 7 and lowest accuracy for AUs 1 and 6.

Hybrid system. We obtained the best performance when we combined all three sources of information into a single neural network. The classifier was a feed-forward network with 10 hidden units taking 50 component projections, five feature measures, and six template matches as input. The hybrid system improved the generalization performance to 90.9%, over the best individual method at 88.6%. While the increase is small, it constitutes about 20% of the difference between the best individual classifier and perfect performance.

We examined how the hybrid system benefited from the multiple sources of input information by looking at correlations in the performances of the three individual classifiers. The contribution of additional inputs to the signal-to-noise ratio depends on their correlations. Each data point in the correlation was mean percent correct for 1 of the 20 faces, across all actions and action magnitudes. The performances of the holistic and the flow field classifiers were correlated, $r^2 = 0.36$, $t(18) = 2.96$, $p < .01$. The feature-based system was not correlated with either the holistic or flow field classifiers, $r^2 = 0.05$, $t(18) = 0.85$, $p > .4$, and $r^2 = 0.02$, $t(18) = 0.65$, $p > .5$, respectively. Although the stand-alone performance of the feature-based system was low, it contributed to the hybrid system by providing estimates that were not correlated with the two template-based systems. Without the feature measures, 17% of the improvement was lost.

Human subjects. A benchmark for the performance of the automated systems was provided by the performance of naive human subjects on the same set of images with identical cropping and scaling. Human nonexperts classified the images with 73.7% accuracy. This is a difficult classification problem that requires considerable training for people to be able to perform well. Performance of the naive human subjects was significantly lower than that of the hybrid system on the subset of images used in the human study ($Z = 2.04$, $p < .05$).

A second benchmark was provided by the agreement rates of expert coders on these images. The expert human subjects classified the actions with 91.8% agreement with the class labels assigned during database collection, which is well above the FACS intercoder agreement standard for proficiency. The majority of the disagreement was on the low-magnitude examples of the actions, and the absence of video motion could account for much of the disagreement. Because the images were originally labeled by two expert coders with access to stop-motion video, these data provide a measure of intercoder agreement between coding stop-motion

Table 2. Confusion Matrix for the Automated Classifiers

Action unit	Responses																							
	AU 1				AU 2				AU 4				AU 5				AU 6				AU 7			
	Hol	Mt	Ft	Hyb																				
AU 1	.58	.20	.50	.57	.19	.31	.04	.17	.00	.00	.29	.01	.10	.33	.14	.08	.03	.00	.00	.00	.10	.15	.02	.18
AU 2	.12	.02	.10	.10	.83	.94	.36	.85	.01	.00	.04	.00	.01	.02	.41	.00	.00	.00	.00	.03	.02	.09	.05	
AU 4	.00	.00	.08	.00	.00	.01	.01	.00	.96	.97	.54	.99	.00	.00	.26	.00	.06	.00	.00	.04	.02	.10	.01	
AU 5	.01	.00	.07	.00	.15	.00	.35	.00	.00	.00	.10	.00	.98	1.0	.74	1.0	.00	.00	.00	.00	.00	.06	.00	
AU 6	.00	.00	.00	.00	.00	.00	.02	.00	.00	.16	.00	.02	.06	.04	.20	.02	.56	.40	.38	.74	.38	.40	.40	.22
AU 7	.00	.00	.06	.00	.00	.00	.03	.00	.01	.00	.06	.01	.00	.02	.21	.01	.00	.03	.03	.00	.99	.94	.62	.98

Note: Values are the percent occurrence of each response for a given action. Hol = holistic; Mt = motion; Ft = feature; Hyb = hybrid.

video and static images. The performance of the holistic and hybrid computer systems did not differ significantly from that of the human experts ($Z = 1.63, 1.86$), but the expert coders did outperform the optic flow and feature-based classifiers ($Z = 3.17, p < .01$; $Z = 7.2, p < .001$).

Error analysis. The action confusions made by both naive and expert human subjects are presented in Table 1. Naive subjects made the most confusions between AUs 6 and 7, which both alter the appearance underneath the eye, followed by AUs 2 and 5, which both give an eye widening appearance by raising the outer brows and the upper lid, respectively, followed by AUs 1 and 2, which raise the inner and outer portions of the eyebrows, respectively. The majority of the disagreements for the experts were between AUs 6 and 7.

Table 2 shows the action confusions made by the three image analysis systems and the hybrid system. Correlations among the action confusions are given in Table 3. Consistent with the performance rate comparisons, the confusions made by the holistic system were highly correlated with those of the motion-based system, whereas the confusions made by the feature-based system were less closely correlated with those of the holistic system and not correlated with those of the motion-based system.

Of the four automated systems, the holistic system had the pattern of confusions most similar to those of both the naive human subjects and the expert coders. This finding is consistent with previous reports that principal component representations of face images account well for human perception of distinctiveness and recognizability of faces (Hancock, Burton, & Bruce, 1996; O’Toole, Deffenbacher, Valentin, & Abdi, 1994). The confusions of the

feature-based system were least correlated with those of the human subjects, with a low but significant correlation with those of the expert coders and no significant correlation with the naive subjects.

Discussion

Facial action codes provide a rich description of facial behavior that enables investigation of the relationship of facial behavior and internal state. We developed methods for automatically classifying facial actions from image sequences. The approach presented here differed from that of other computer facial expression analysis systems in that we focused on classifying the basic elements that comprise complex facial movements rather than on classifying emotion categories. Classification was learned directly from images of facial actions without mediation of a physical model.

We compared the performance of three diverse approaches to processing face images for classifying facial actions: holistic spatial analysis, feature measurement, and analysis of motion flow fields. Best performance of 92% correct for classifying six actions was achieved by combining the three methods of image analysis into a single system. The hybrid system classified an image in less than 1 s on a 120-MHz Pentium processor. Our initial results are promising because some of the upper facial actions included in this study require extensive training for humans to discriminate reliably. The holistic and hybrid automated systems outperformed human nonexperts on this task, and the hybrid system performed as well as highly trained experts.

The image analysis methods did not depend on the precise number of video frames nor did the actions need to be of any particular magnitude beyond the neutral frame. For applications in which neutral images are unavailable, PCA could be performed on the original gray-level images. Methods based on PCA have successfully classified static gray-level images of facial expressions (Padgett & Cottrell, 1997). The image analysis also required localization of the face in the image. For this study, the localization was carried out by making two mouse clicks, one at the center of each eye, in the first frame of the sequence. All other aspects of the systems were fully automated. Highly accurate eye location algorithms are available (e.g., Beymer, 1994), and automating this step is a realistic option. The image alignment procedure ignored out-of-plane rotations, which could be handled by methods for estimating the frontal view of a face from a nonfrontal view (e.g., Beymer et al., 1993; Vetter & Poggio, 1997).

There are 46 action units, of which we have presented classification results for 6. The holistic and motion-based systems are

Table 3. Action Confusion Correlations

	Expert	Holistic	Motion	Feature	Hybrid
Naive	.58***	.36**	.18*	.05	.19*
Expert		.66***	.36**	.23**	.36**
Holistic			.70***	.17*	.82***
Motion				.09	.69***
Feature					.07

Note: Entries are squared correlation coefficients. Significance is based on a *t*-test with *df* = 28.
p* < .05. *p* < .01. ****p* < .001.

not specific to particular actions and can be applied to any other facial motion. The image analysis in these systems was limited to the upper half of the face because upper facial actions have little effect on motion in the lower face, and vice versa (Ekman & Friesen, 1978). We are presently applying these techniques to images of the lower half of the face to classify the lower facial actions.

It remains an empirical question to determine whether this approach will have the same success when dealing with spontaneous rather than deliberately made facial actions. Although the morphology of the facial actions should not differ in spontaneous as compared with deliberate facial actions, the timing of the activity and the complexity of facial actions may well be different. Evaluating spontaneous facial movement is an important next step.

Cohn et al. (in press) developed a related system for automatic facial action coding that takes advantage of the precision obtainable through human-computer interaction. In their system, more than 40 feature points are manually identified in the initial image. The system presented here is more automatable because human interaction in our system was limited to the two mouse clicks in the initial image. Another difference between the two systems is that the Cohn et al. system estimates displacements in a select set of feature points, whereas our system captures full-field information on skin motion.

Most automatic facial expression analysis systems have focused on either motion or surface gray levels but not on both. Although human subjects can recognize facial expressions from motion signals alone (Bassili, 1979), recognition rates are only just above chance. Likewise, although humans can recognize facial expressions quite well from static gray-level images, expression recognition improves with high temporal resolution video (Wallbott, 1992). This system integrates analysis of both surface gray levels and motion information.

The two template-based methods, holistic spatial analysis and motion analysis, outperformed the feature-based method for facial action recognition. This finding supports previous findings that template approaches outperformed feature-based systems for recognizing faces (Brunelli & Poggio, 1993; Lanitis et al., 1997). This result is also supported by the work of Lien (1998), who found that facial furrow measurement based on analysis of high image gradients was not as accurate as full field motion analysis for facial action classification.

Our results also suggest that hand-crafted features plus templates may be superior to either one alone, because their performances may not be correlated. Classification of local feature measurements is heavily dependent on exactly which features

were measured. Padgett and Cottrell (1997) found that local PCA was superior to full-face eigenfaces for expression recognition. These local features were based on data-driven kernels obtained from the gray levels of the face images, as opposed to the hand-crafted feature measures that performed poorly in this study and others (e.g., Brunelli & Poggio, 1993). We are presently exploring local representations of faces based on the outputs of local filters such as Gabor wavelets and local PCA for facial action classification.

A completely automated method for scoring facial actions in images would make facial expression measurement more widely accessible as a research tool in behavioral science, medicine, and psychophysiology. Facial action codes have already proven a useful behavioral measure in studies of emotion (e.g., Ekman, 1984), human interaction and communication (e.g., Ekman & Oster, 1979), cognition (e.g., Zajonc, 1984), and child development (e.g., Camras, 1977). Measurement of observable facial behavior has been combined with simultaneous scalp EEG in the study of physiological patterns associated with emotional states (e.g., Davidson, Ekman, Saron, Senulis, & Friesen, 1990) and with measures of autonomic nervous system activity to study the relationship of emotion to facial muscles and the autonomic nervous system (Ekman, Levenson, & Friesen, 1983).

Neuropsychological investigations in humans and physiological recordings in primates have indicated a separate neural substrate for recognizing facial expression independent of identity (Tranel, Damasio, & Damasio, 1988; Adolphs, Tranel, Damasio, & Damasio, 1995; Hasselmo, Rolls, & Baylis, 1989), and there is evidence that the recognition of specific facial expressions depends on distinct systems (e.g., Adolphs, Damasio, Tranel, & Damasio, 1996). Neural substrates for the perception of two negative emotions, fear and disgust, have recently been differentiated using functional magnetic resonance imaging (Phillips et al., 1997). Whereas perception of expressions of fear and anger produced activation in the amygdala (Breiter et al., 1996; Morris et al., 1996), perception of disgust in others activated interior insular cortex, an area involved in responses to offensive tastes (Kinomura et al., 1994; Yaxley, Rolls, & Seinkewitz, 1988).

Automated facial action coding could provide an objective measure of visual stimuli in such investigations of the neural substrates for the perception of facial expressions and could provide a behavioral measure of emotional state. An automated system would improve the reliability, precision, and temporal resolution of facial measurement and would facilitate the use of facial measurement in psychophysiological investigations into the neural systems mediating emotion.

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